

CIVIL-312: Hydraulic Engineering and Infrastructures

# Numerical Modeling in Open Channel Flow

Instructor: Dr. Clemente Gotelli

Sustainable River Engineering, Energy, & Morphodynamics  
(**STREEM**)

GC G1 507

E-mail: [clemente.gotelli@epfl.ch](mailto:clemente.gotelli@epfl.ch)

Fall 2025

- Late HW submissions will incur a 0.5 deduction from the final grade for every day of delay (e.g., after 2 days your maximum grade would be 5/6)
  
- The exercise session of Week 11 (Friday 28/11, 10:00–12:00) will be dedicated to Homework 2, which is due on Week 12, Friday 5/12 at 23:59. There will be no new exercises that day; instead, you will have the opportunity to continue working on HW2 (hopefully you will have started it beforehand) and ask us any questions.
  
- To give you more time, we have decided to release HW3 earlier and extend its deadline.
  - HW3 will be assigned on Week 12, Friday 5/12, and it will be due on 9 January — providing three weeks of work, excluding the holiday break.
  - Exercise session of Week 14 (Friday 14/12) will be dedicated to HW 3 development and questions

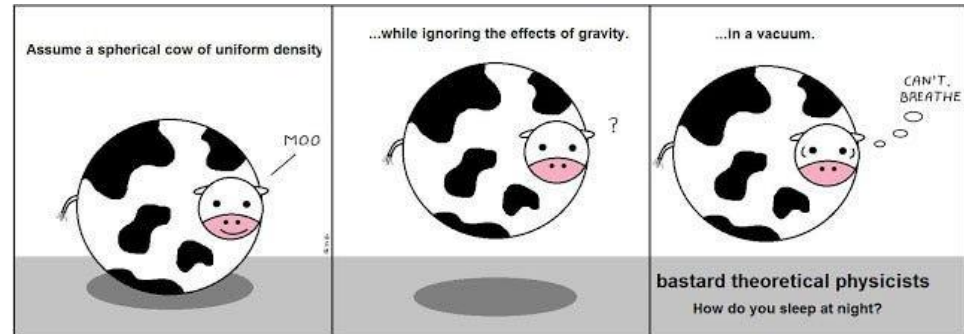
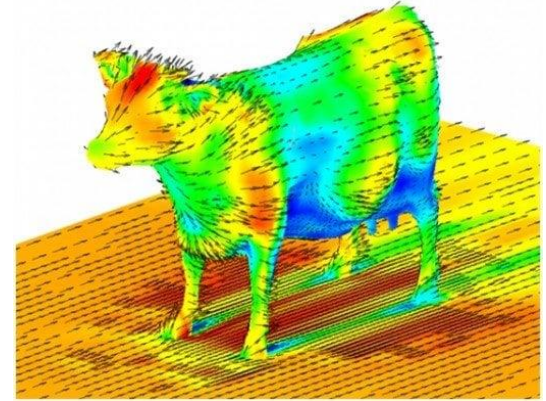
## Fast announcement:

As this is an important workshop, it will be **exceptionally** recorded and published tomorrow on Moodle.

# Today's Agenda

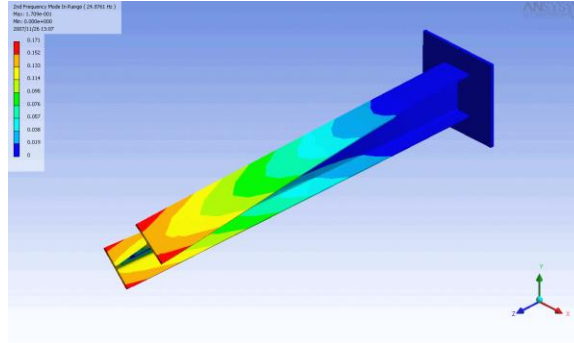
- Introduction to Numerical Modeling in Open Channel Flow
  - Why to model?
  - Different types of models
- Introduction to HEC-RAS
- Homework 2 😊
  - Discussion
  - If time allows, Q&A

- A model as a **simplified mathematical representation** of physical laws.
- Purpose:
  - Prediction,
  - Understanding,
  - Hypothesis testing,
  - Design support.
- The trade-off between **complexity**, **accuracy**, and **computational cost**.

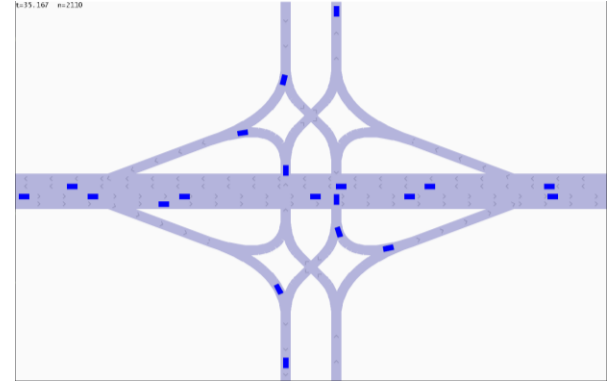




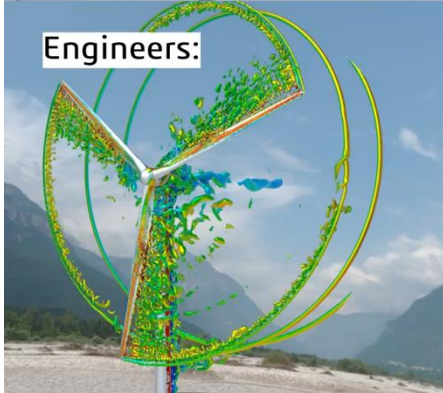
Most People:



Structures



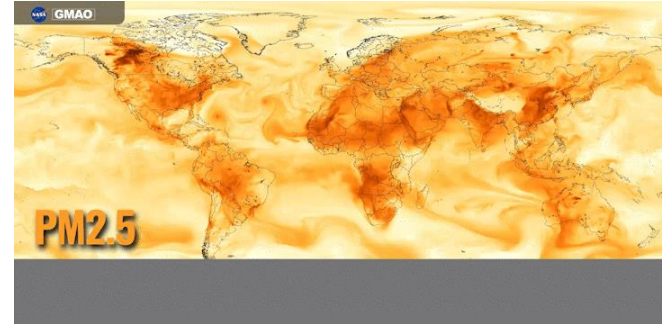
Transport



Engineers:

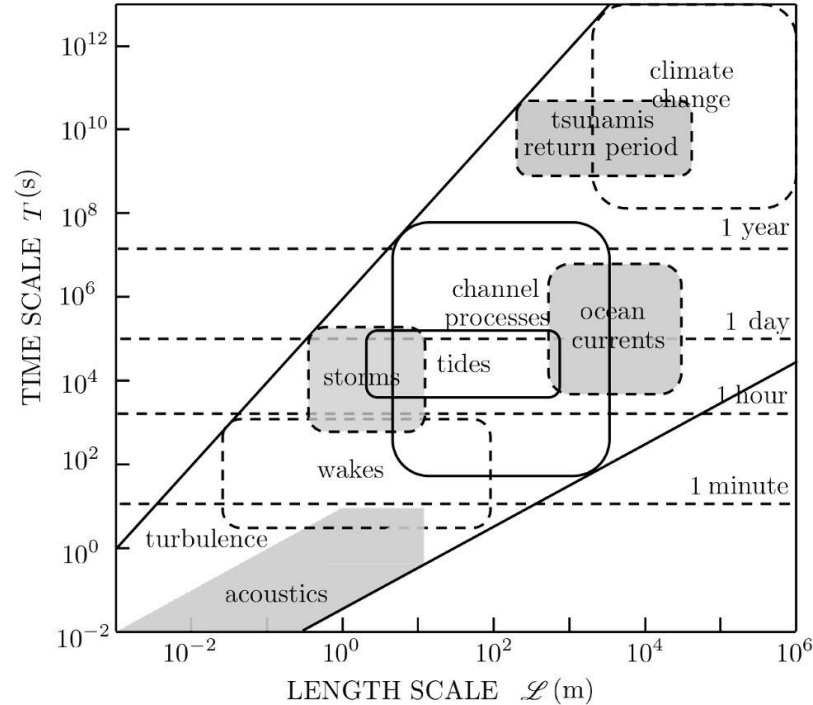


Aerospace

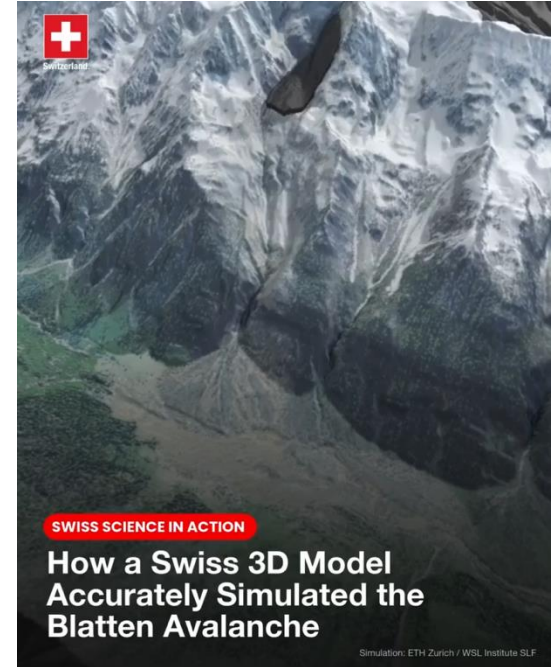
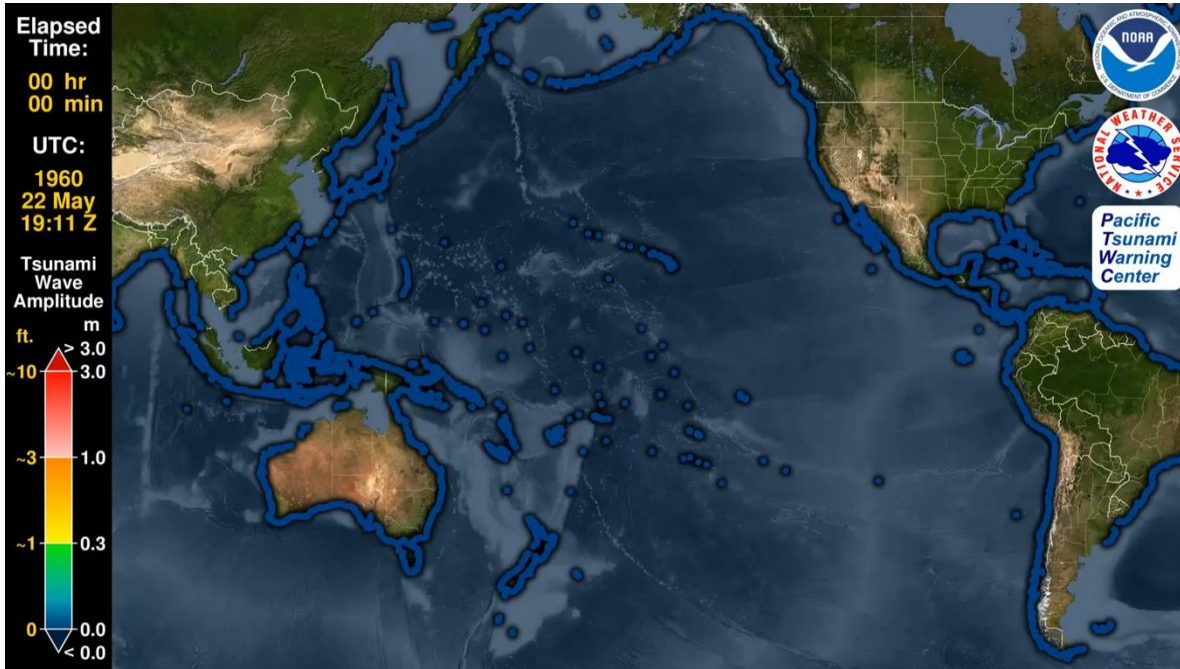


Environment

# Models for Geophysical Flows

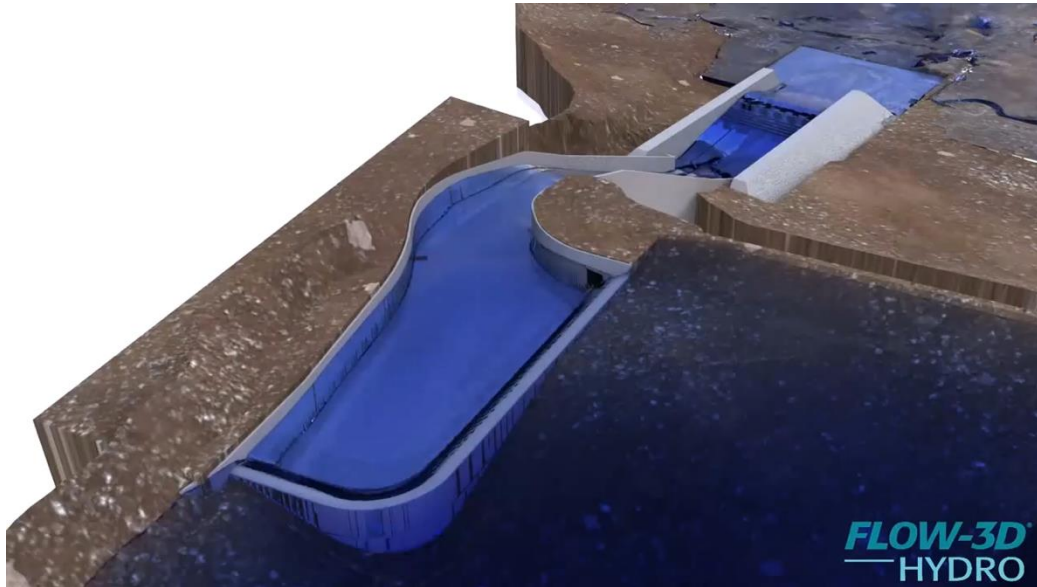


We face problems that vary in both **scale** and **nature**



We face problems that vary in both **scale** and **nature**

- Why Do We Need Models in Open-Channel Hydraulics?
  - Laboratory and field data are limited in time and scale.
  - Models allow exploring “what-if” scenarios under controlled conditions.
  - **The importance of calibration and validation: comparing with measurements.**



- Models are never 100% reliable
- Input data may require assumptions
- Mathematical models may be inadequate
- Accuracy limited by available computing power
- Interpretation and skill of the modeler/engineer

- We solve the same physics with different levels of detail
- In 1D
  - First models available in “software” appeared during the 70’s
  - Still used in professional world for engineering design and regulatory studies with channelized flow.

Equations to solve for a 1D free surface simulation:

$$Q_1 = Q_2 = Q$$

$$z_1 + y_1 + \alpha_1 \frac{V_1^2}{2g} = z_2 + y_2 + \alpha_2 \frac{V_2^2}{2g} + h_f + h_L$$

$$h_f = L S_f$$

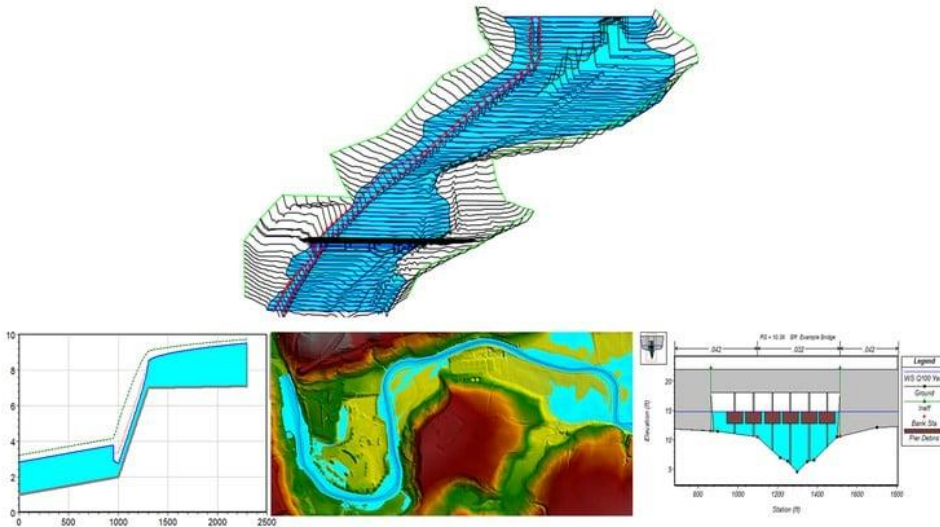
$$S_f = \frac{n^2 Q^2}{A^2 R^{4/3}}$$

$$h_L = C \frac{(V_2^2 - V_1^2)}{2g}$$

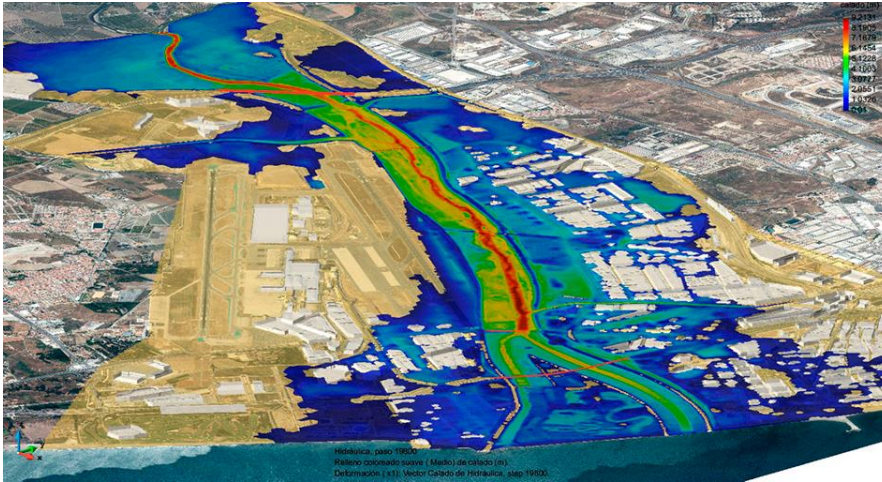
$$S_0 = \frac{z_1 - z_2}{L}$$

$$\frac{dy}{dx} = \frac{S_0 - S_f}{1 - Fr^2}$$

$$Fr^2 = \frac{V^2}{gD}, \quad D = \frac{A}{T}$$



- In 2D
  - Current standard for industry for realistic flood behavior, complex terrain, and safety assessments.
  - Still research being done to improve efficiency and include new features



Equations to solve for a 2D free surface simulation:

$$\frac{\partial h}{\partial t} + \frac{\partial(hu)}{\partial x} + \frac{\partial(hv)}{\partial y} = q$$

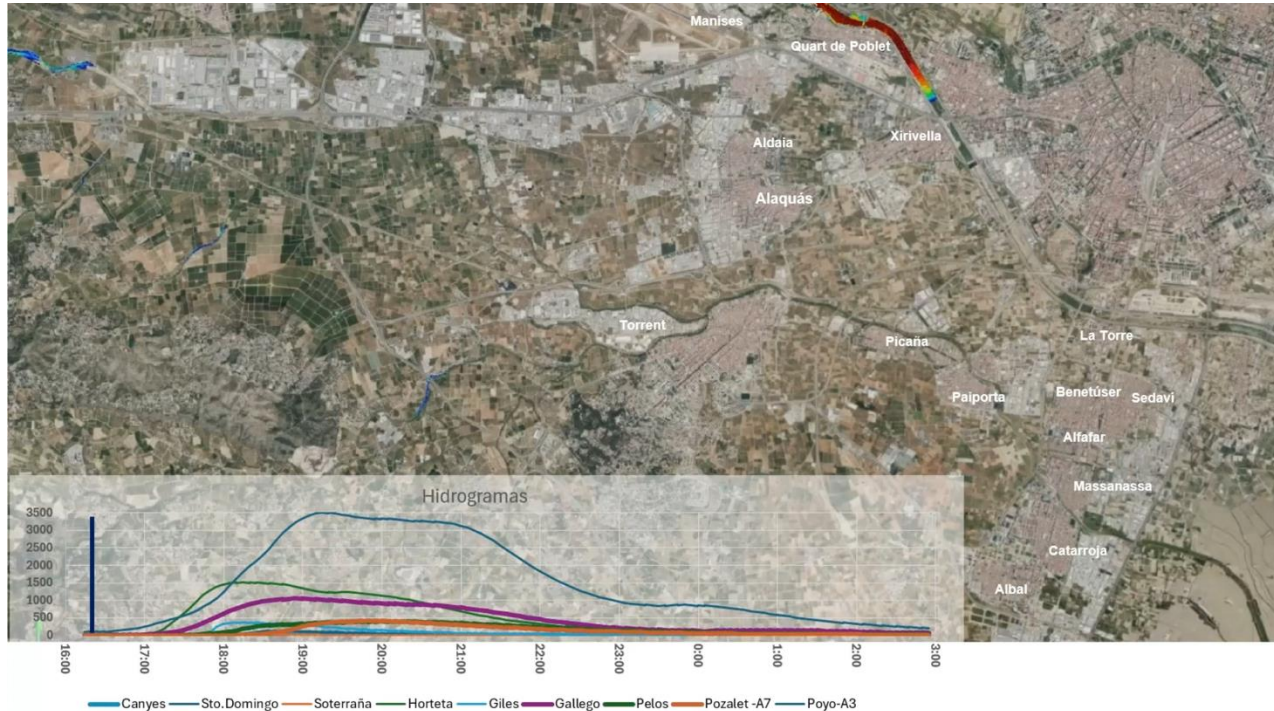
$$\frac{\partial(hu)}{\partial t} + \frac{\partial}{\partial x} (hu^2 + \frac{1}{2}gh^2) + \frac{\partial(huv)}{\partial y} = -gh \frac{\partial z_b}{\partial x} - \tau_{bx}/\rho + qu_x$$

$$\frac{\partial(hv)}{\partial t} + \frac{\partial(huv)}{\partial x} + \frac{\partial}{\partial y} (hv^2 + \frac{1}{2}gh^2) = -gh \frac{\partial z_b}{\partial y} - \tau_{by}/\rho + qv_y$$

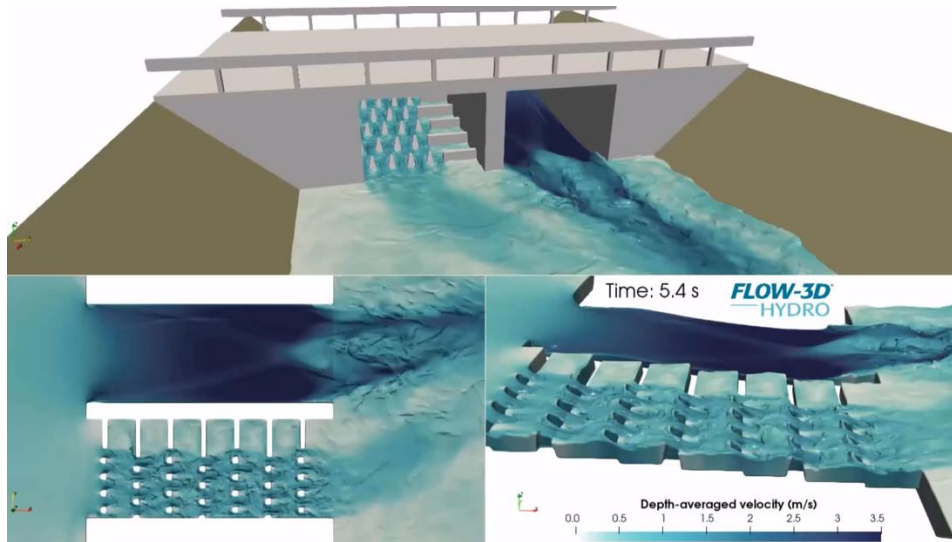
$$\tau_{bx} = \rho g n^2 \frac{u\sqrt{u^2 + v^2}}{h^{1/3}}, \quad \tau_{by} = \rho g n^2 \frac{v\sqrt{u^2 + v^2}}{h^{1/3}}$$

$$S_{fx} = \frac{n^2 u \sqrt{u^2 + v^2}}{h^{4/3}}, \quad S_{fy} = \frac{n^2 v \sqrt{u^2 + v^2}}{h^{4/3}}$$

- In 2D
  - Current standard for industry for realistic flood behavior, complex terrain, and safety assessments.
  - Still research being done to improve efficiency and include new features



- In 3D
  - Mostly for research or very specific small scale professional applications
  - Very expensive in computation power



Equations to solve for a 3D free surface simulation:

$$\nabla \cdot \mathbf{u} = 0$$

$$\frac{\partial(\rho\mathbf{u})}{\partial t} + \nabla \cdot (\rho\mathbf{u} \otimes \mathbf{u}) = -\nabla p + \nabla \cdot [\mu_{\text{eff}}(\nabla\mathbf{u} + (\nabla\mathbf{u})^T)] + \rho\mathbf{g} + \mathbf{F}_\sigma$$

$$\mathbf{F}_\sigma = \sigma\kappa\nabla\alpha$$

$$\kappa = -\nabla \cdot \left( \frac{\nabla\alpha}{|\nabla\alpha|} \right)$$

$$\frac{\partial\alpha}{\partial t} + \nabla \cdot (\alpha\mathbf{u}) = 0$$

$$\rho = \alpha\rho_1 + (1 - \alpha)\rho_2$$

$$\mu = \alpha\mu_1 + (1 - \alpha)\mu_2$$

$$\frac{\partial(\rho k)}{\partial t} + \nabla \cdot (\rho k\mathbf{u}) = \nabla \cdot \left[ \left( \mu + \frac{\mu_t}{\sigma_k} \right) \nabla k \right] + P_k - \rho\varepsilon$$

$$\frac{\partial(\rho\varepsilon)}{\partial t} + \nabla \cdot (\rho\varepsilon\mathbf{u}) = \nabla \cdot \left[ \left( \mu + \frac{\mu_t}{\sigma_\varepsilon} \right) \nabla \varepsilon \right] + C_{1\varepsilon} \frac{\varepsilon}{k} P_k - C_{2\varepsilon} \rho \frac{\varepsilon^2}{k}$$

$$\mu_t = C_\mu \rho \frac{k^2}{\varepsilon}$$

$$\frac{\partial(\rho h)}{\partial t} + \nabla \cdot (\rho h\mathbf{u}) = \nabla \cdot (k_{\text{eff}} \nabla T) + S_h$$

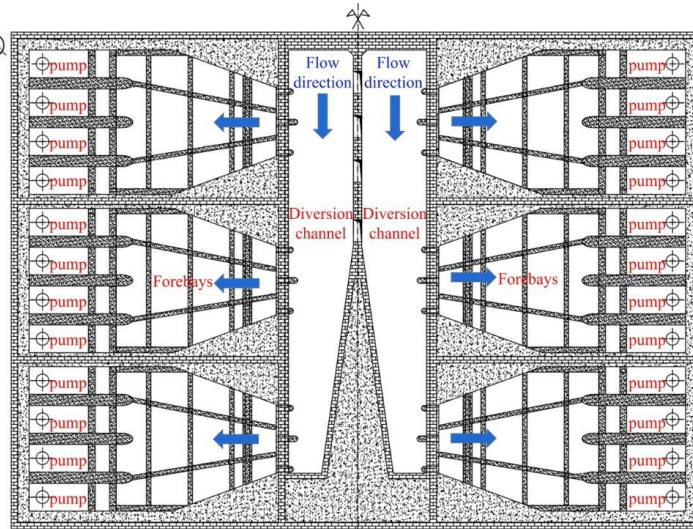
- In 3D: [example](#)



(a)



(b)



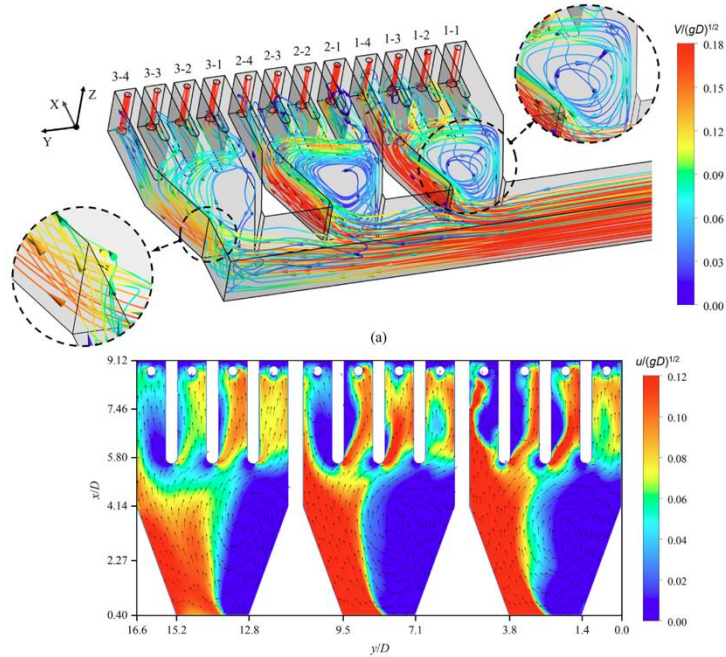
(c)

Reasons for the deterioration of hydraulic characteristics in the forebays:

- Flow recirculation,
- Helical mainstream and
- Vortex strip

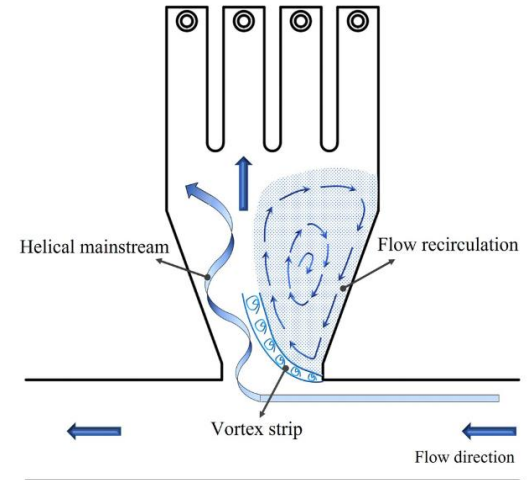
Wuhaogou Pumping Station in China

- In 3D: example



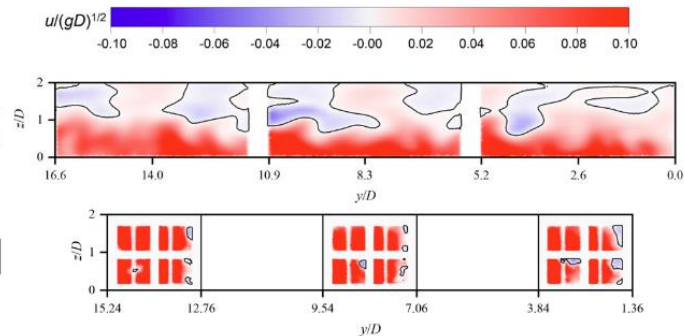
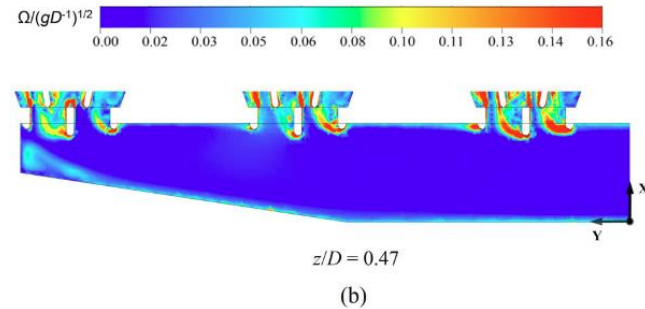
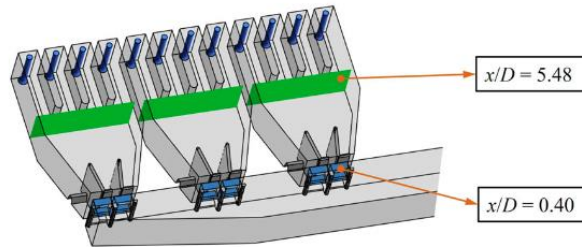
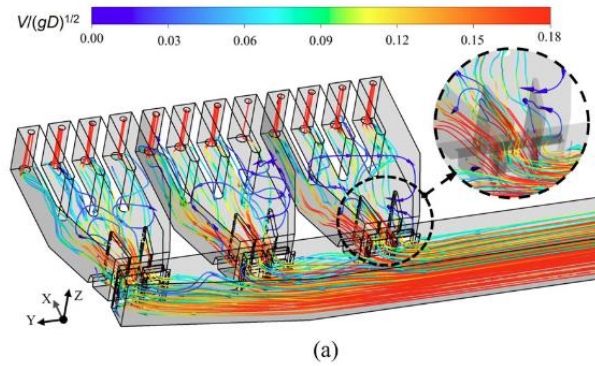
Reasons for the deterioration of hydraulic characteristics in the forebays:

- Flow recirculation,
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- Vortex strip



- In 3D: [example](#)

We can test multiple options that would otherwise be very costly.



- Many software programs
- All of them with different:
  - Set of equations
  - Boundary conditions
  - Extra features
  - Performance
  - Accuracy
  - **Assumptions**
- We must understand **how the model operates** and **what assumptions it makes** to:
  - **Decide when each model is appropriate** for the problem we want to solve.
  - **Recognize its limitations** and avoid interpreting results beyond its scope.
  - **Select meaningful input data** that are consistent with the model's assumptions.
  - **Interpret outputs critically**, knowing what processes are included and what are not.
- And remember: **don't believe everything that comes out of a software**



US

Iber  
ES

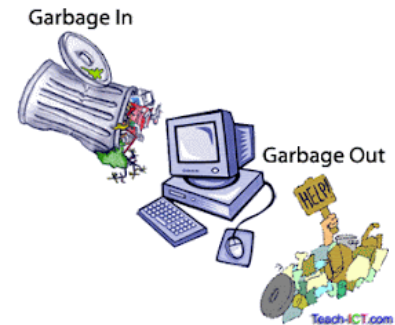
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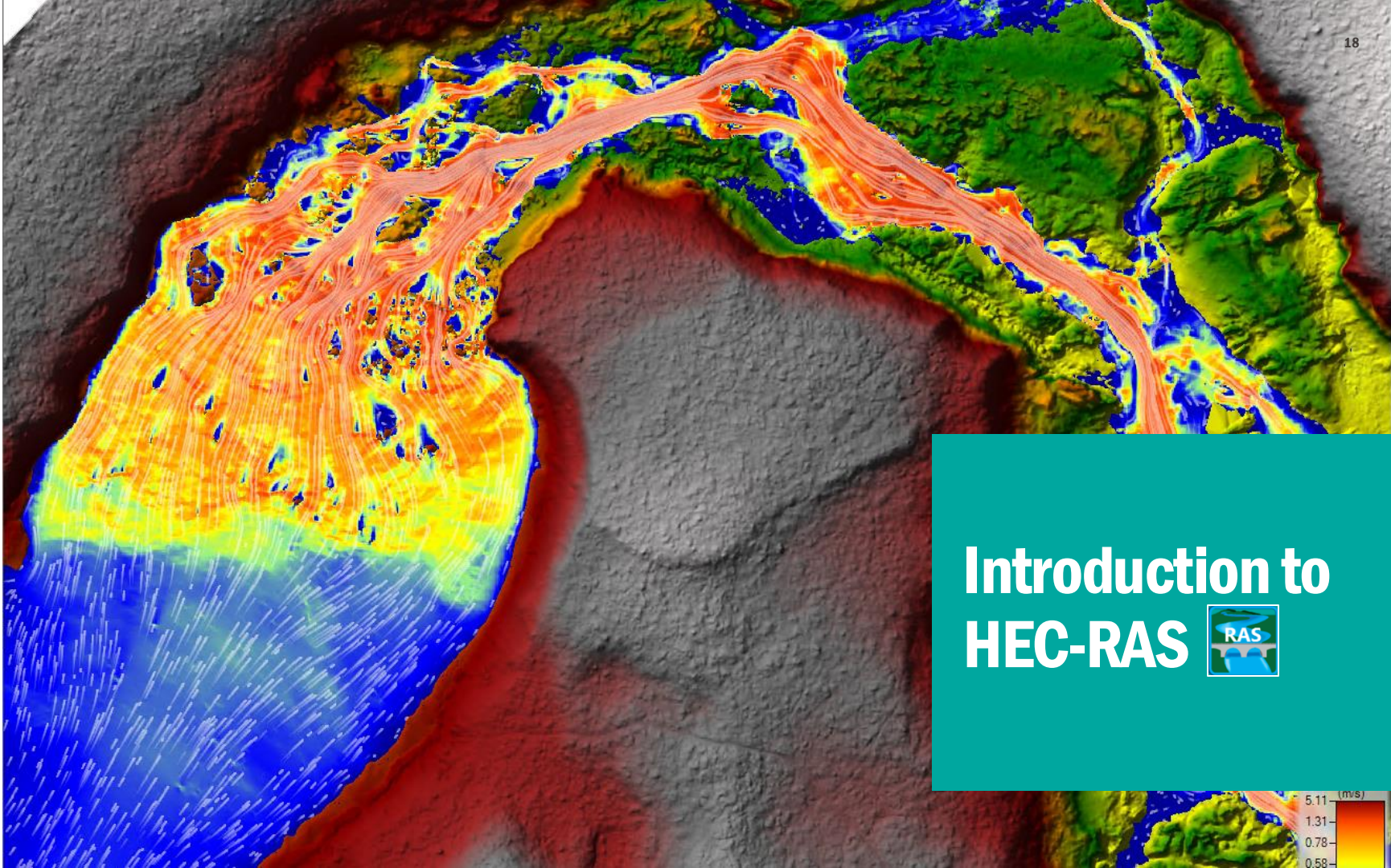
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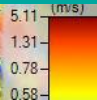
NL



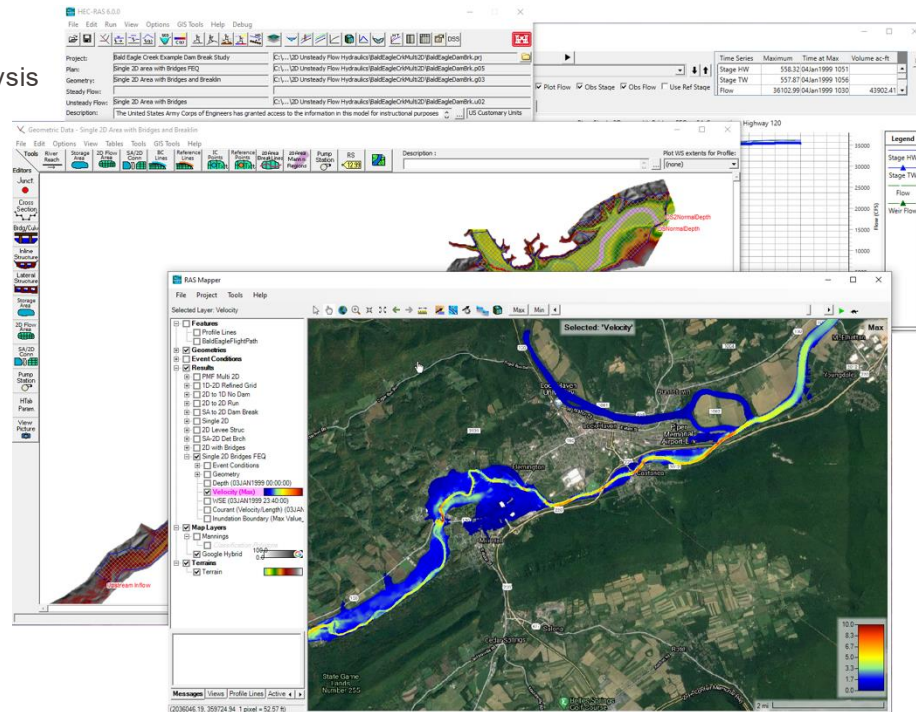
*All models are wrong, but some are useful.* — George Box



# Introduction to HEC-RAS



- Hydrologic Engineering Center's River Analysis System (HEC-RAS)
- Developed by the U.S. Army Corps of Engineers (USACE): **it's free!**
- Key Capabilities:
  - One-dimensional (1D) **steady** and **unsteady** flow analysis
  - Two-dimensional (2D) unsteady flow modeling
  - Sediment transport and mobile bed computations
  - Water quality and temperature modeling
  - Floodplain mapping and inundation visualization
- Applications:
  - Flood risk assessment and management
  - Bridge and culvert hydraulic design
  - Dam break and levee breach simulations
  - Environmental and restoration studies
- Widely used worldwide in both academic research and professional engineering practice



# Steady vs Unsteady flow simulations

## ▪ **Steady Flow** → For this course

Use when conditions are **relatively constant over time**

Ideal for:

- **Bridge/Culvert design**
- **Floodplain mapping (regulatory studies)**
- **Simple canal systems**

**Advantages:** Quick setup, fast computation, easier calibration

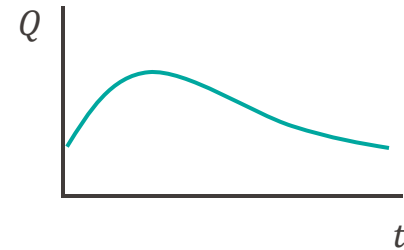
## ▪ **Unsteady Flow** → During the Master's (?)

Use when flow or stage **changes with time**

Ideal for:

- **Flood routing / storm events**
- **Dam break or levee breach analysis**
- **Reservoir or tidal system modeling**

**Advantages:** Captures dynamic flow behavior, storage, and wave effects



## ▪ Steady Flow

Use when conditions are **relatively constant over time**

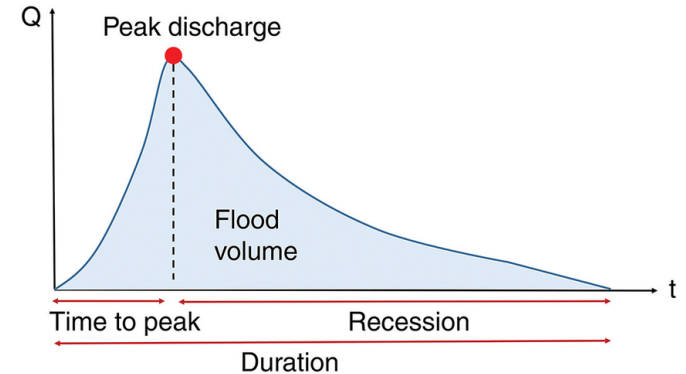
Ideal for:

- **Bridge/Culvert design**
- **Floodplain mapping (regulatory studies)**
- **Simple canal systems**

**Advantages:** Quick setup, fast computation, easier calibration

**Limitations of 1D steady flow conditions:**

- Simple canal systems
- Dominant flows in  $x$  direction (1-D)
- Channel slopes less than 10%
- Velocity and WS constant across cross-section
- Cross-section does not change (no erosion or deposition).



- Before we computed the hydraulic profile with

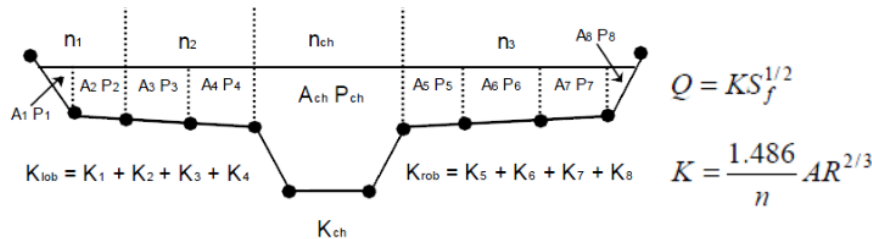
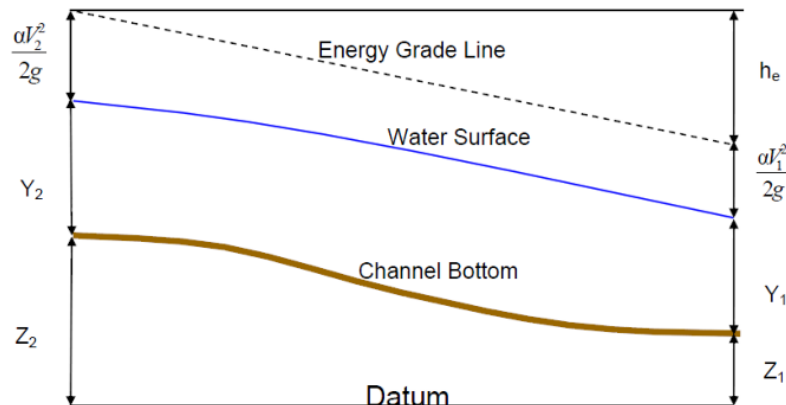
$$\frac{dy}{dx} = \frac{S_0 - S_f}{1 - Fr^2}$$

- In HEC-RAS, water surface profiles are computed by solving the Energy equation between two consecutive cross-sections (1 and 2) using an iterative procedure called **standard step method**

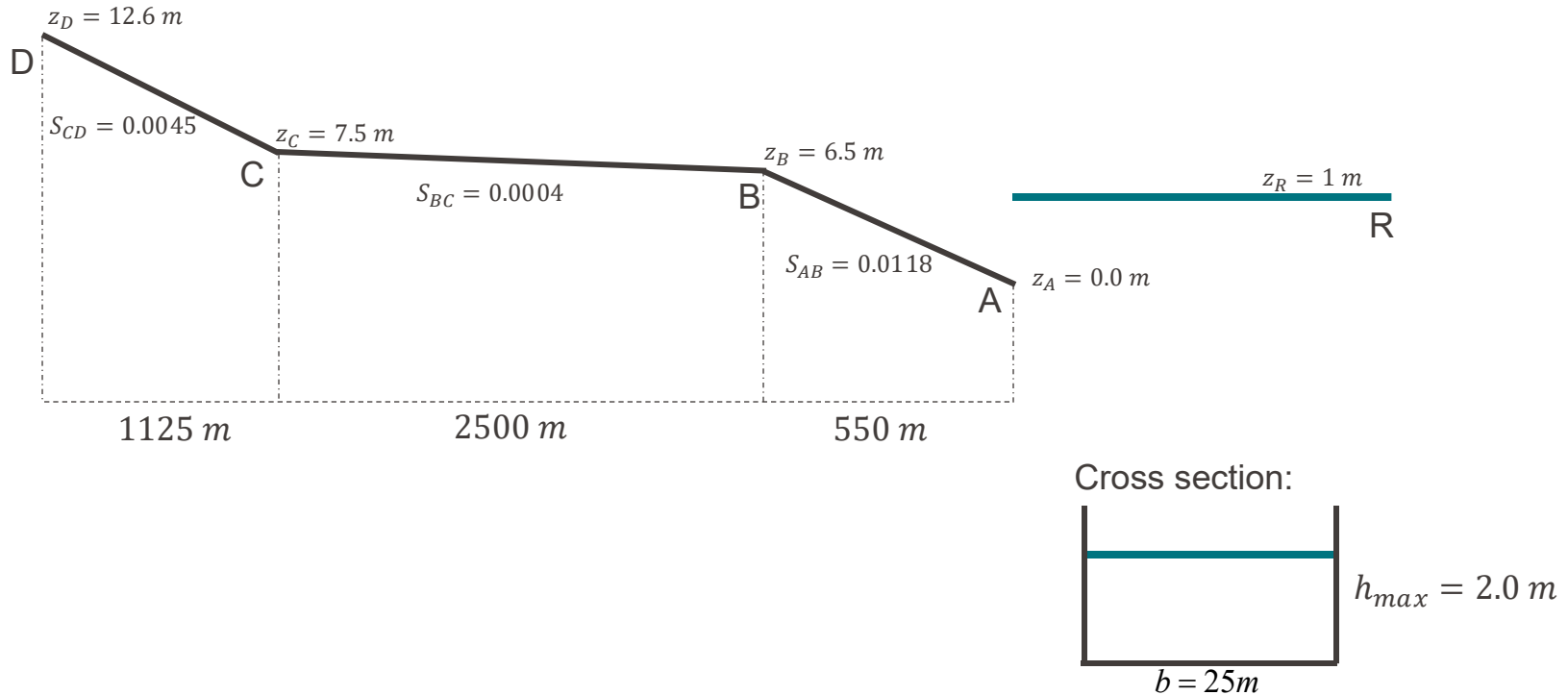
$$Z_2 + Y_2 + \alpha \frac{U^2}{2g} = Z_1 + Y_1 + \alpha \frac{U_1}{2g} + h_e$$

- Energy losses** include:
  - Friction (from Manning's equation)
  - Local losses (expansion/contraction)

$$h_e = LS_f + C \left[ \frac{\alpha_2 V_2^2}{2g} - \frac{\alpha_1 V_1^2}{2g} \right]$$



- The regulated irrigation channel has a flow rate of  $35 \text{ m}^3/\text{s}$ . The elevation of the water surface at the end of the channel is fixed by a reservoir. Draw the hydraulic profiles and simulate the system in HEC-RAS 1D.



- The regulated irrigation channel has a flow rate of  $35 \text{ m}^3/\text{s}$ . The elevation of the water surface at the end of the channel is fixed by a reservoir. Draw the hydraulic profiles and simulate the system in HEC-RAS 1D.

Parameter	Magnitude	Units
Q	35	$\text{m}^3/\text{s}$
Width b	25	m
Roughness	0.01	

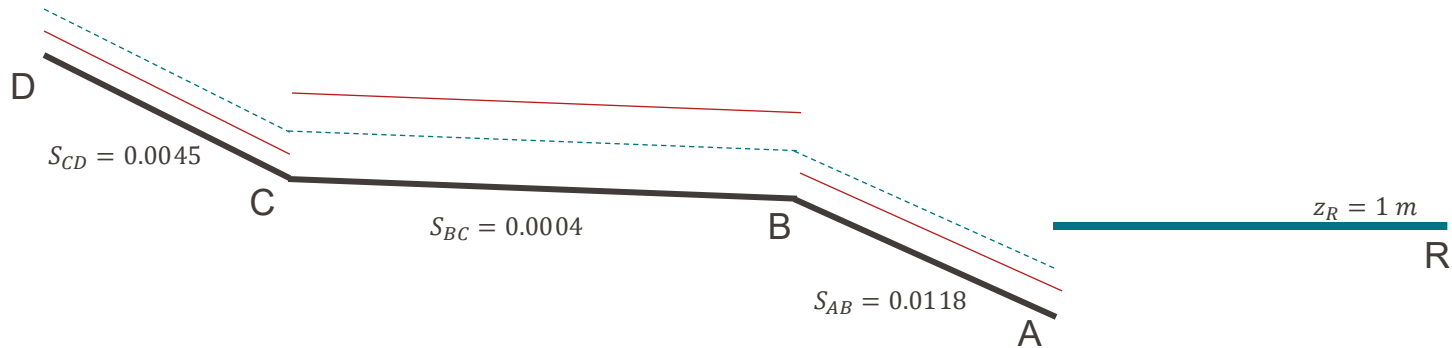
### Critical Depth

$$y_c = \sqrt[3]{\frac{q^2}{g}} = \sqrt[3]{\frac{Q^2}{b^2 g}} = 0.59 \text{ m}$$

### Normal Depth

$$Q = \frac{1}{n} \frac{(b \cdot y_n)^{5/3}}{(b + 2 \cdot y_n)^{2/3}} S_o^{1/2}$$

Subreach	(m)
CD	0.395
BC	0.828
AB	0.295



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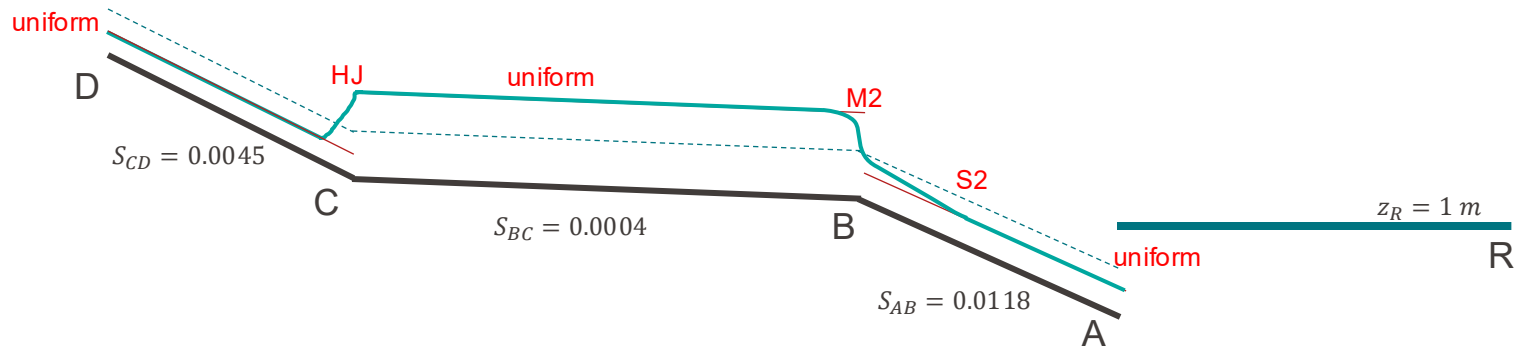
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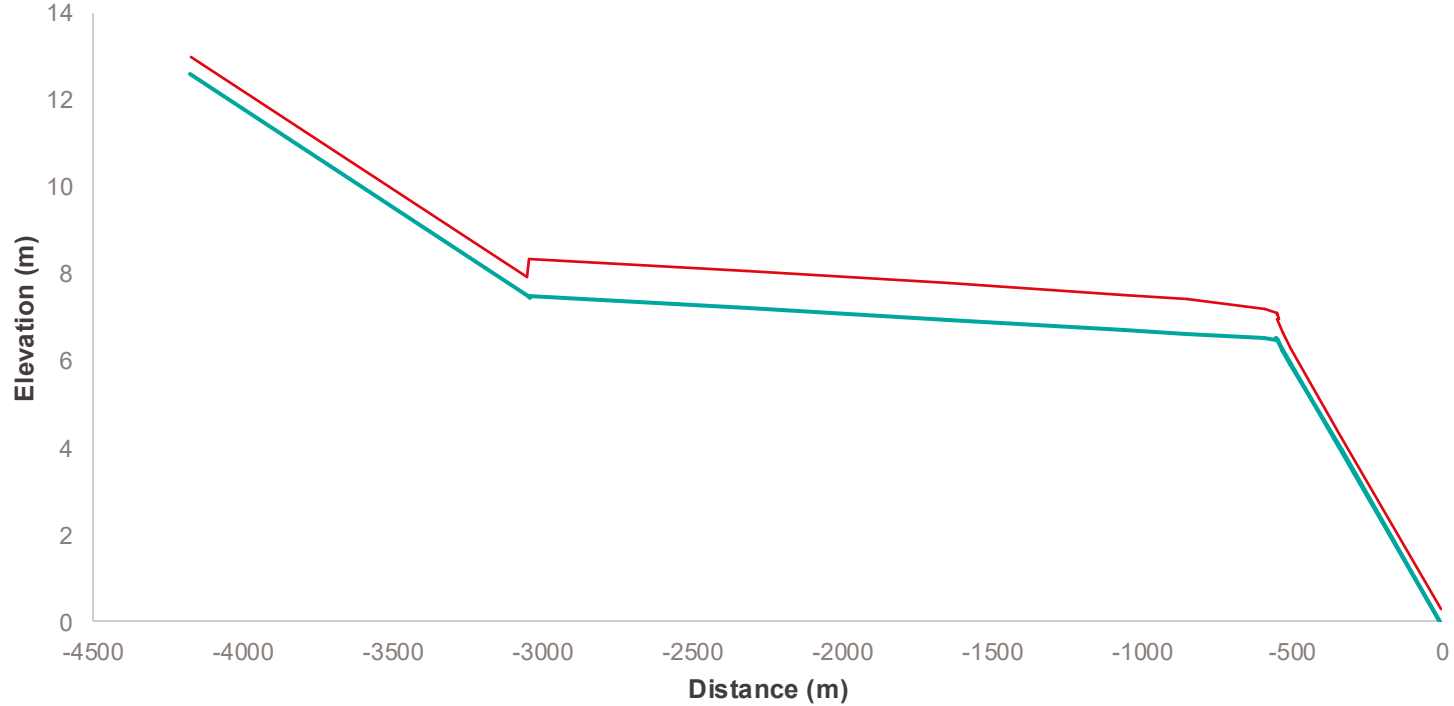
### Normal Depth

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Subreach	(m)
CD	0.395
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- Solving with Direct-Step Method we get:



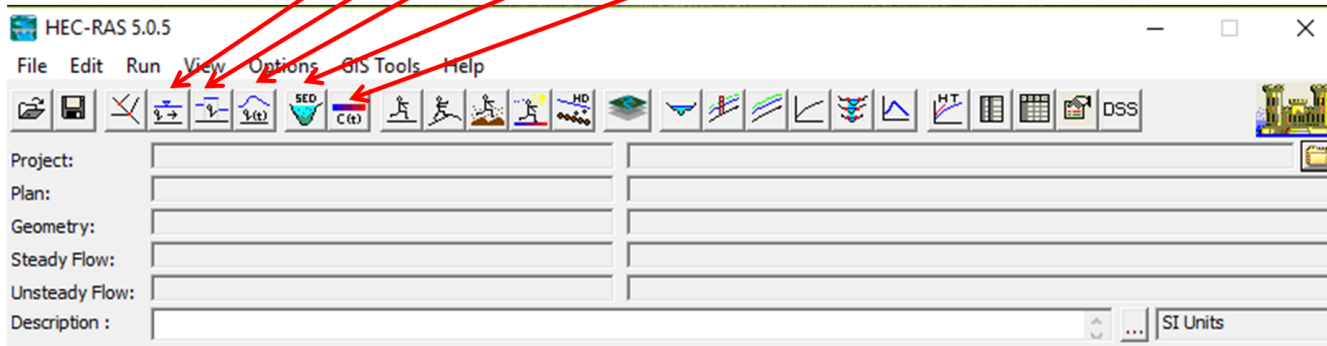
## HEC-RAS Modules

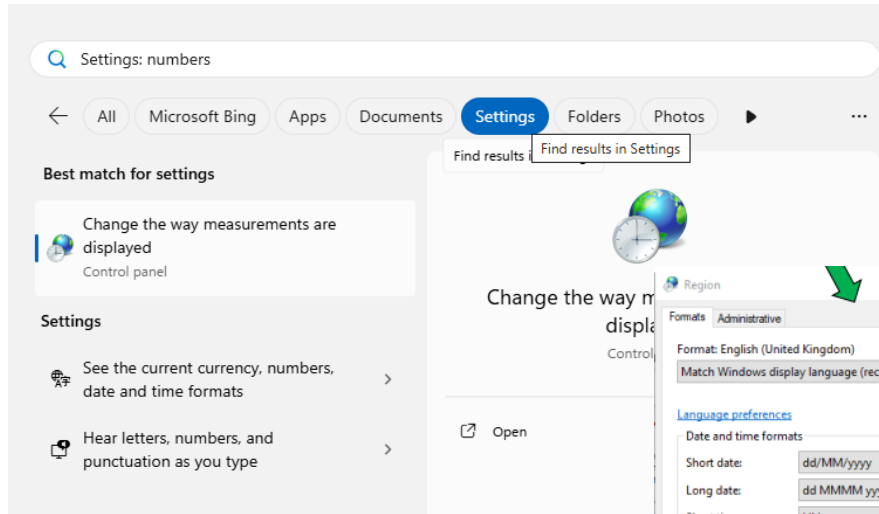
## 1. Hydraulic Analysis

- Steady state
- Quasi-unsteady state
- Unsteady state

## 2. Sediment Transport

## 3. Water Quality

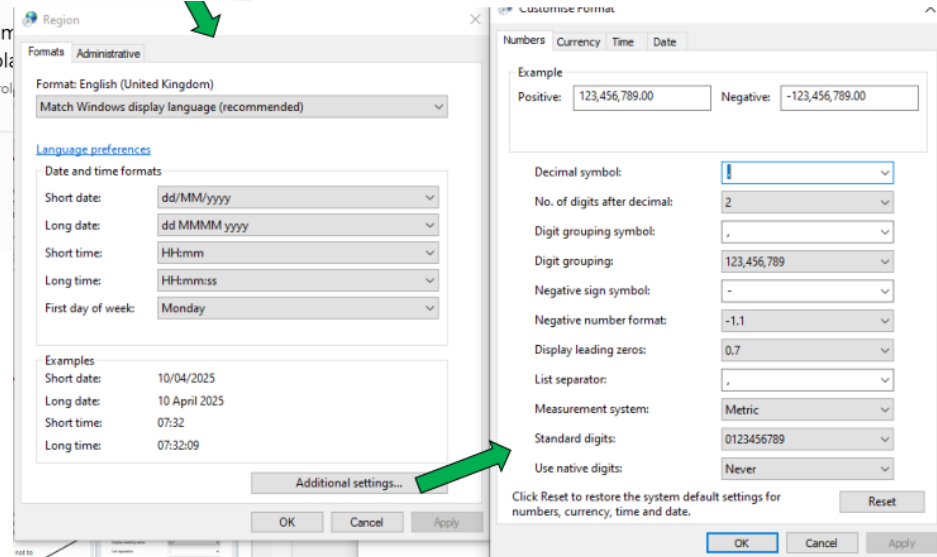


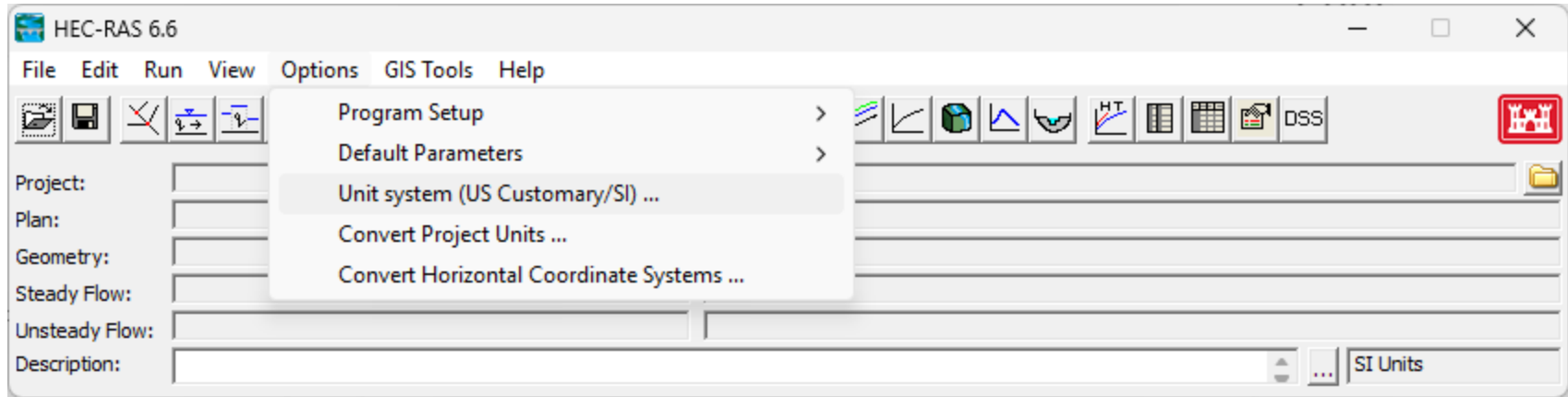


EPFL's VDI is already in US format

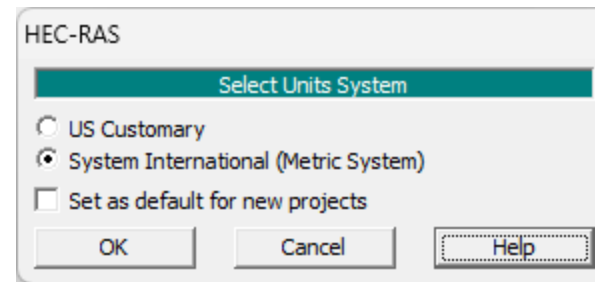
Pay attention to regional format.  
It should be set like in the US:

“.” (dot) as decimal symbol

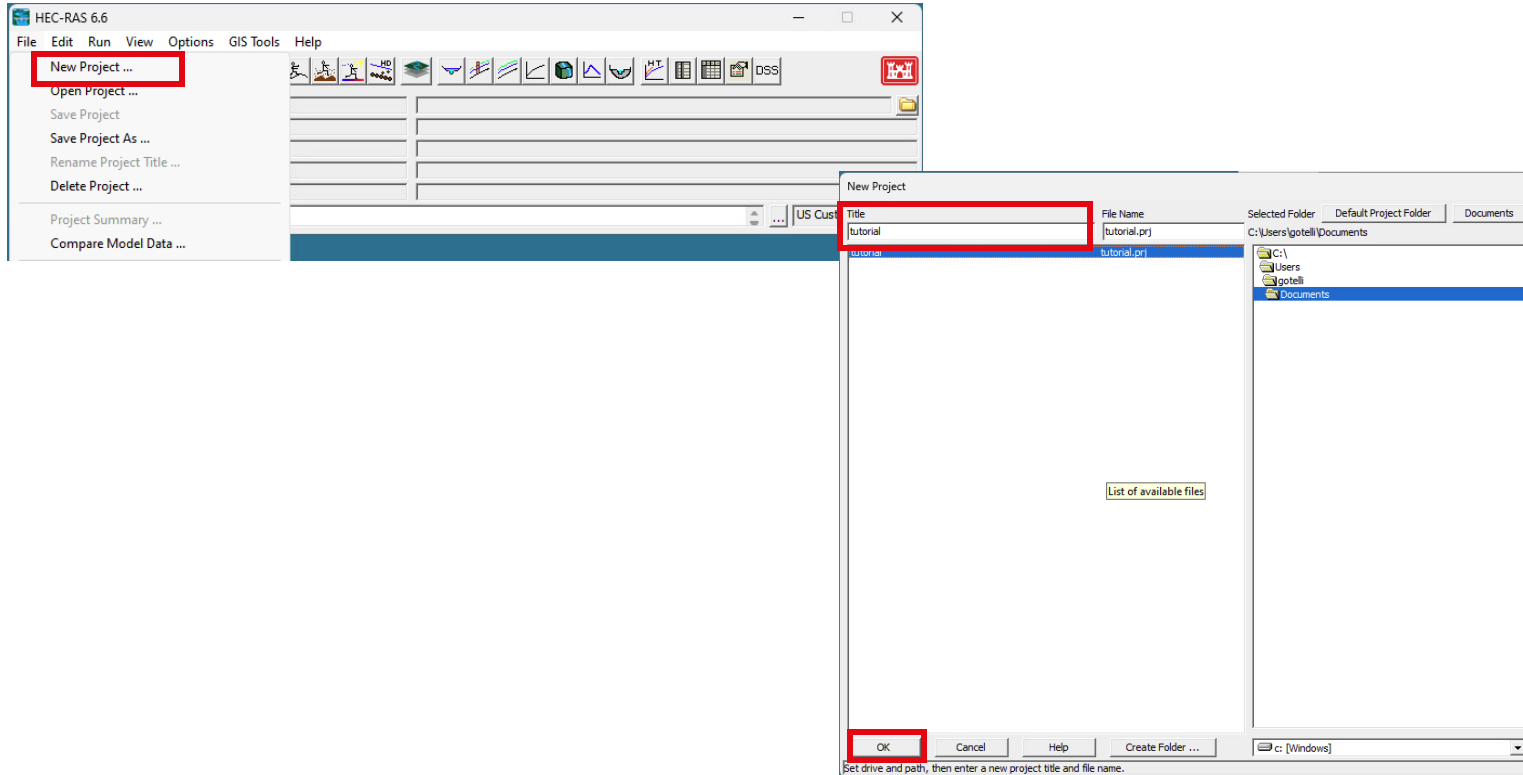




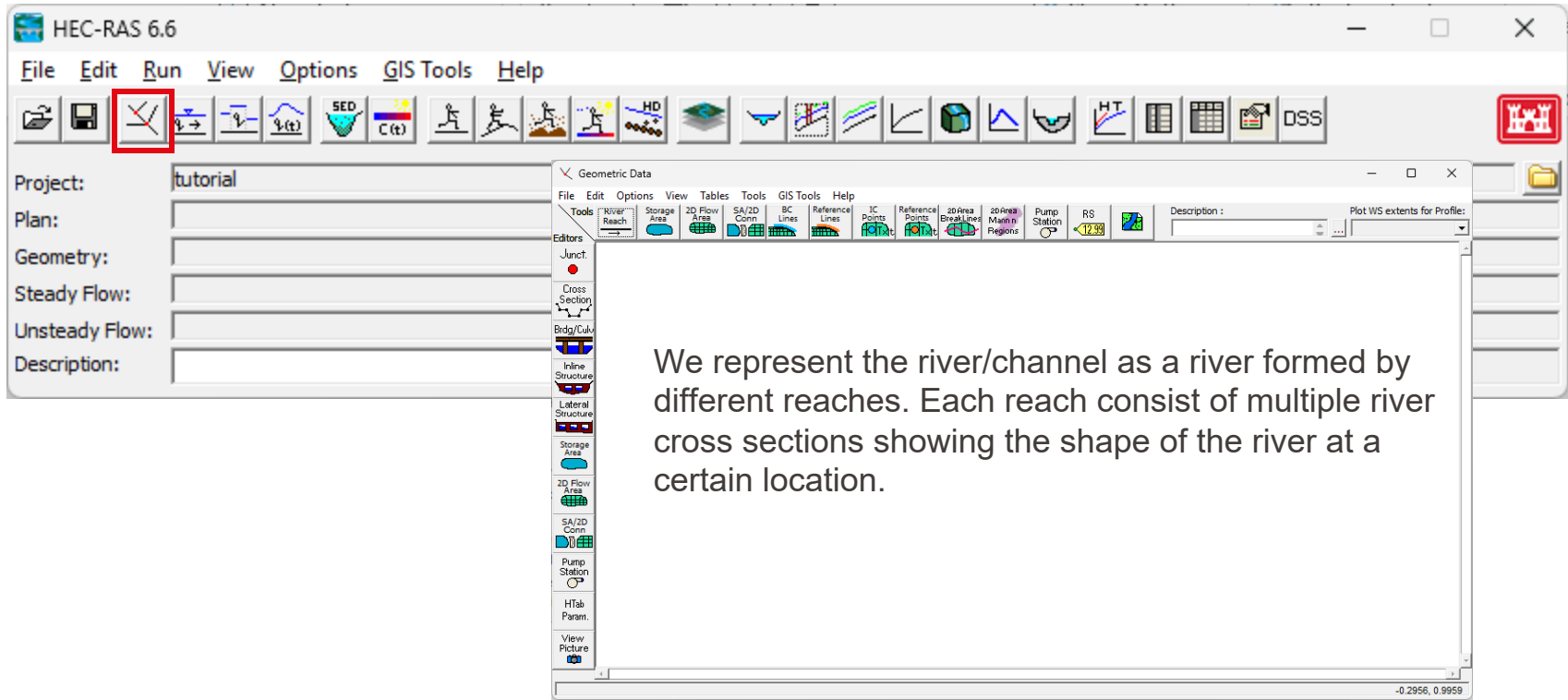
We check the Unit System



## New project



We open the Geometry Editor:



River Reach → We create the line representing the river. Complete River and Reach names.

The image displays two screenshots of the HEC-RAS Geometric Data window. The top screenshot shows the 'River Reach' tool highlighted in the 'Tools' menu. The bottom screenshot shows the 'River Reach' tool selected, with a dialog box open for naming the river and reach. The dialog box contains the following text:

Select existing River or enter a new River name (16 Char Max), and enter Reach name (16 Char Max).

River: EPFL

Reach: Tutorial

OK Cancel

The bottom screenshot also shows a blue line representing the river reach in the workspace, with a label 'Tutorial' and an arrow indicating the direction of flow. A red text box at the bottom of the window reads: "Some schematic data outside default extents (see View/Set Schematic Plot Extents...)"

We open the Cross Section editor

The screenshot shows the HEC-RAS software interface. The main window is titled "Geometric Data" and contains a toolbar with various editing tools. The "Editors" panel on the left has the "Cross Section" icon highlighted with a red box. A red line is drawn across the main workspace, representing a cross-section line. A red arrow points from the "Cross Section" icon to the "Cross Section Data" editor window.

The "Cross Section Data" window is open, showing the following data:

River: EPFL  
 Reach: Tutorial  
 River Sta.: [ ]

Table: Cross Section Coordinates

Station	Elevation
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
11	

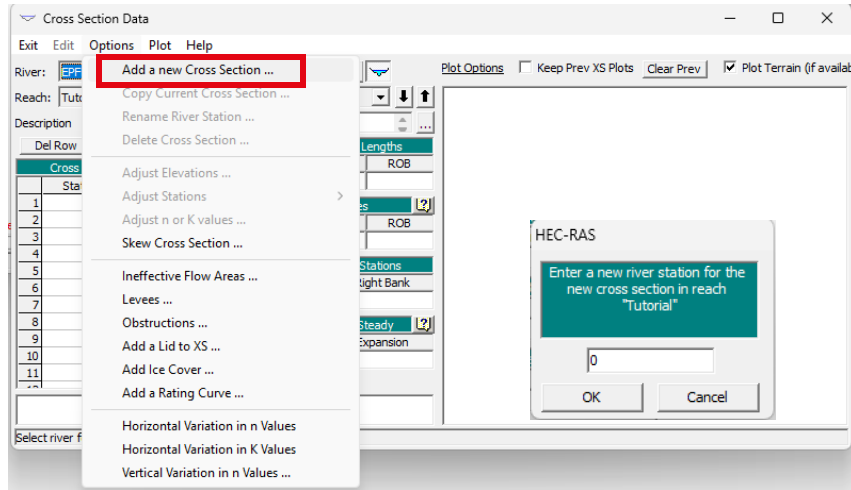
Other parameters in the editor include:

- Downstream Reach Lengths: LOB, Channel, ROB
- Manning's n Values: LOB, Channel, ROB
- Main Channel Bank Stations: Left Bank, Right Bank
- Cont'Exp Coefficient (Steady): Contraction, Expansion

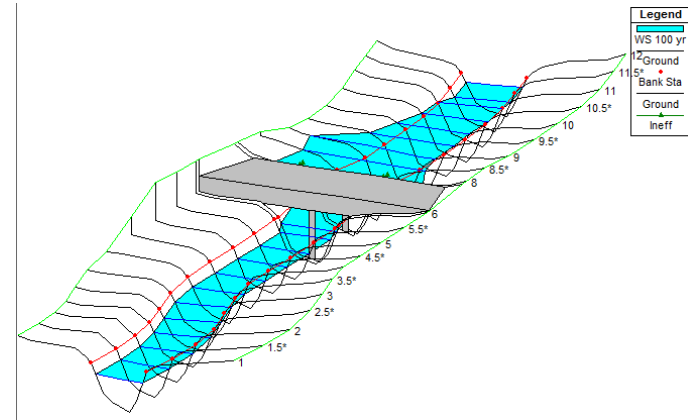
The main plot area of the editor displays "No Data for Plot".

We add a new Cross Section. The river station should be at “0”.

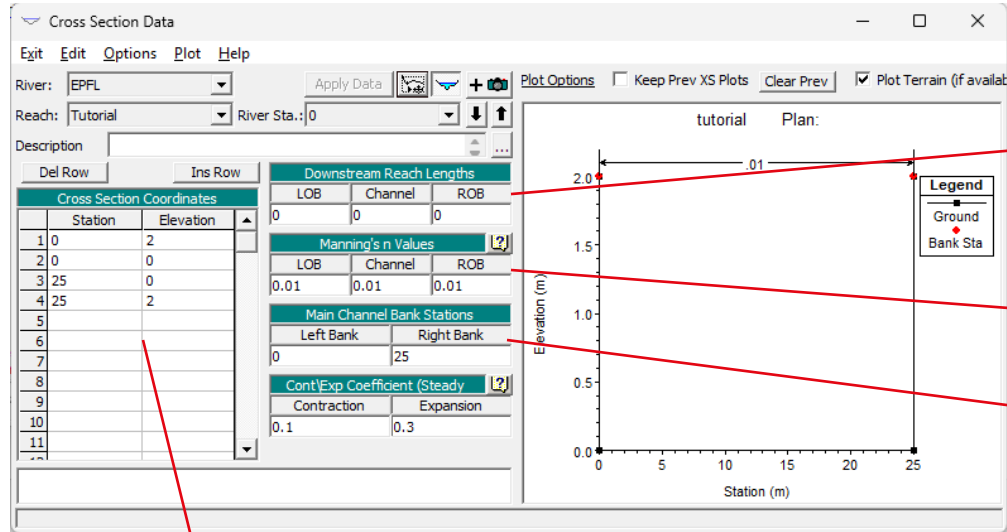
We then fill the section characteristics: points, manning, reach lengths, etc.



A Cross Section is a transversal “cut” of the river



We add a new Cross Section. The river station should be at “0”.  
We then fill the section characteristics: points, manning, reach lengths, etc.

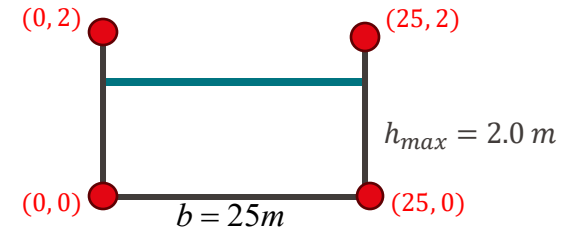


Distance from this section to the next downstream section. We build the channel from downstream to upstream.

Manning values for main channel and flooding zones ( $n = 0.01$ )

Stations defining main channel

We start building the section from the left bank looking downstream.



We add another Cross Section. The new river station should be at “550”.

The screenshot displays the HEC-RAS software interface. The main window is titled "Cross Section Data" and shows a list of cross sections. The "Copy Current Cross Section ..." option is highlighted in red. A "Copy Cross Section" dialog box is open in the foreground, showing the "River Sta" field set to 550.

**Cross Section Data Dialog Box:**

- River: EPFL
- Reach: Tutorial
- Description: Del Row
- Table:

Cross	Sta
1	0
2	0
3	25
4	25
5	
6	
7	
8	
9	
10	
11	
- Menu items:
  - Add a new Cross Section ...
  - Copy Current Cross Section ...**
  - Rename River Station ...
  - Delete Cross Section ...
  - Adjust Elevations ...
  - Adjust Stations
  - Adjust n or K values ...
  - Skew Cross Section ...
  - Ineffective Flow Areas ...
  - Levees ...
  - Obstructions ...
  - Add a Lid to XS ...
  - Add Ice Cover ...
  - Add a Rating Curve ...
  - Horizontal Variation in n Values
  - Horizontal Variation in K Values
  - Vertical Variation in n Values ...

**Copy Cross Section Dialog Box:**

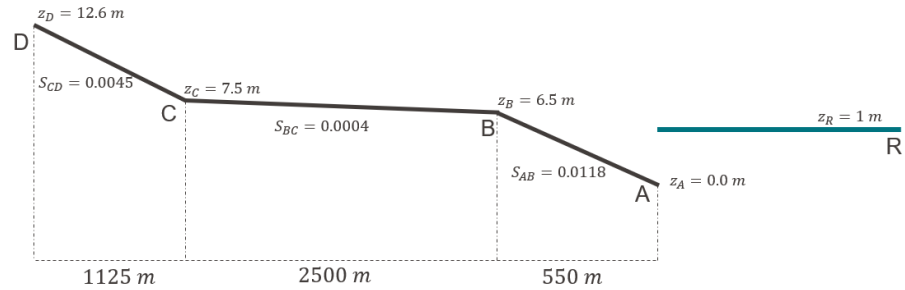
- Select a River and Reach and then enter a new river station.
- River: EPFL
- Reach: Tutorial
- River Sta: 550
- Buttons: OK, Cancel

**Plot Options:**

- Keep Prev XS Plots:
- Clear Prev: [button]
- Plot Terrain (if available):

**Plot:** tutorial Plan: Elevation (m) vs. Stationing. Legend: Ground (black square), Bank Sta (red diamond). A distance of .01 is indicated between two points on the plot.

As the section shape is the same, we just need to adjust the elevation.



Cross Section Data

River: EPFL  
Reach: Tutu  
Description: Del Row

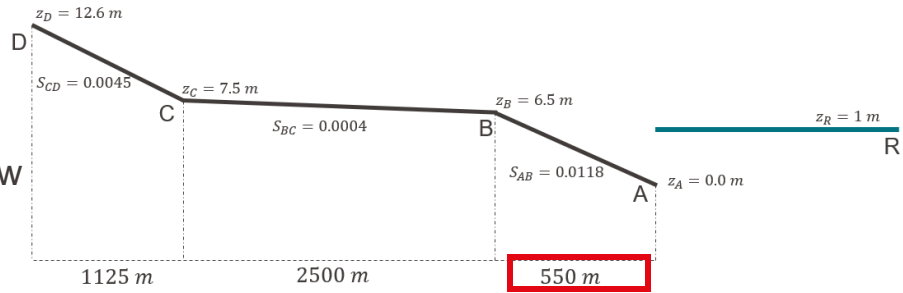
Plot Options:  Keep Prev XS Plots  Clear Prev  Plot Terrain (if available)

Legend: Ground (black square), Bank Sta (red diamond)

HEC-RAS dialog: Enter amount to add to Elevations (+/-) [6.5]

# HEC-RAS: Geometry

Now we need to set the distance from this new cross section to the previous.



Cross Section Data - geo

Exit Edit Options Plot Help

River: EPFL Apply Data Plot Options Keep Prev XS Plots Clear Prev Plot Terrain (if avail)

Reach: Tutorial River Sta.: 550

Description

Cross Section Coordinates		Downstream Reach Lengths		
Station	Elevation	LOB	Channel	ROB
1	0	8.5	550.	550.
2	0	6.5		
3	25	6.5		
4	25	8.5		
5				
6				
7				
8				
9				
10				
11				

Manning's n Values		
LOB	Channel	ROB
0.01	0.01	0.01

Main Channel Bank Stations	
Left Bank	Right Bank
0	25.

Cont\Exp Coefficient (Steady)	
Contraction	Expansion
0.1	0.3

Legend

- EG PF 1
- WS PF 1
- Crit PF 1
- Ground
- Bank Sta

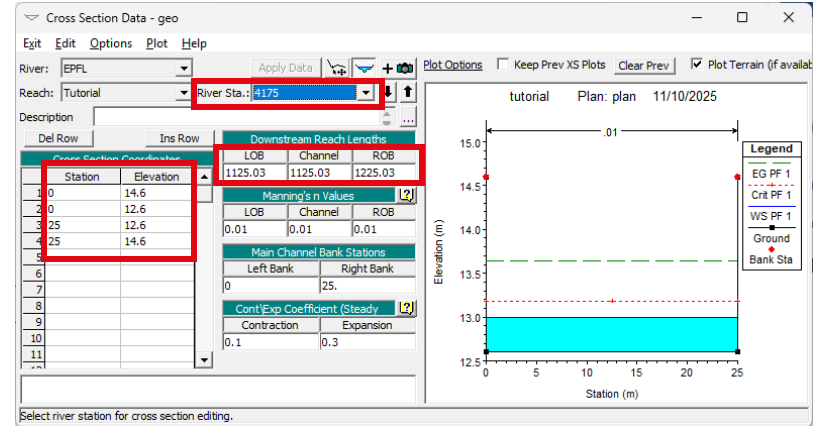
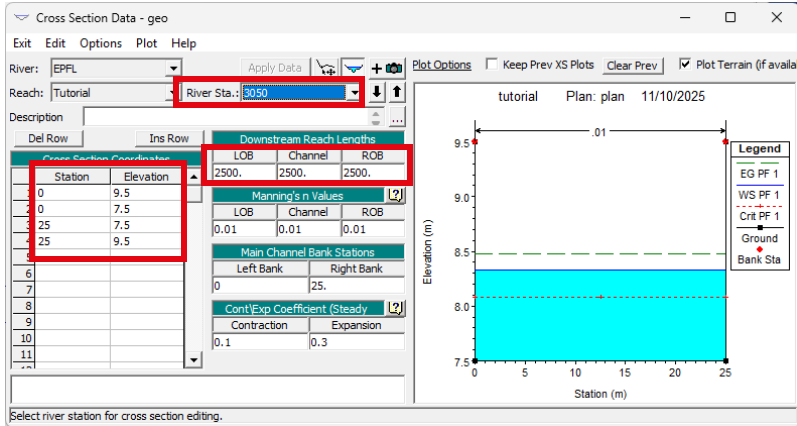
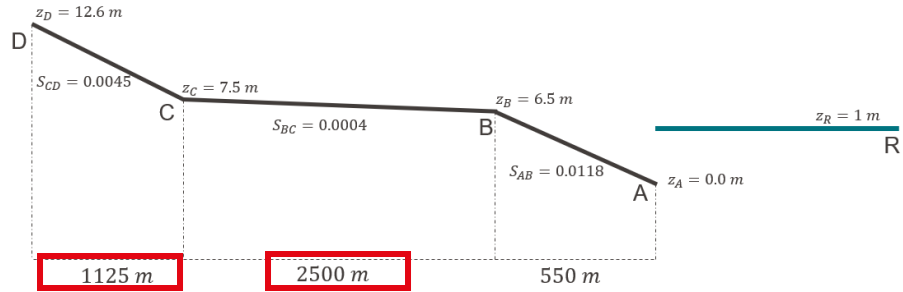
Station (m)

Elevation (m)

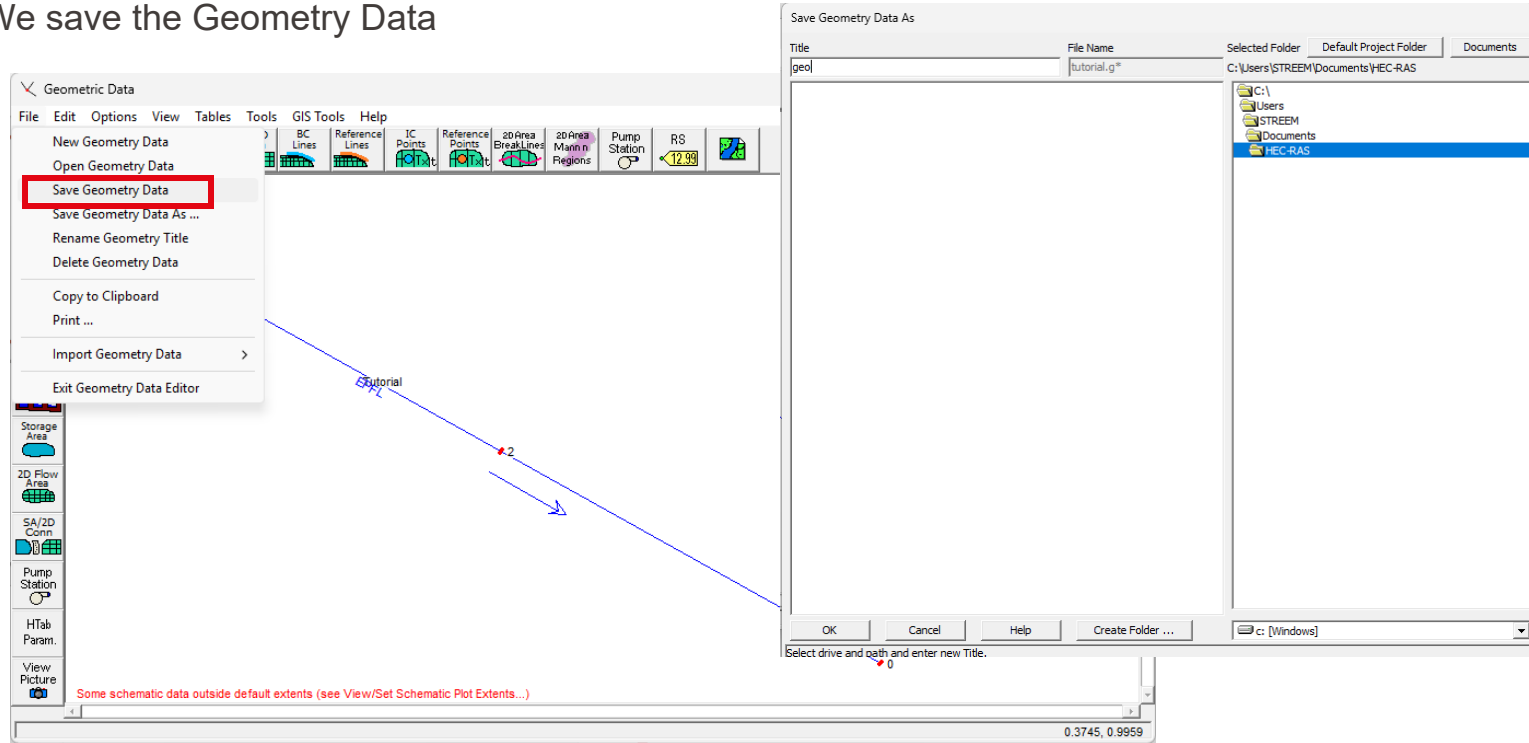
Enter to move to next upstream river station location

# HEC-RAS: Geometry

We repeat for sections at C and D, naming them “3050” and “4175”, respectively.



We save the Geometry Data



Now we add water to the channel. Steady flow simulation.

HEC-RAS 6.6

File Edit Run View Options GIS Tools Help

Project: tutorial

Plan:

Geometry:

Steady Flow:

Unsteady Flow:

Description:

Steady Flow Data - flow

File Options Help

Description :

Enter/Edit Number of Profiles (32000 max): 1 Reach Boundary Conditions ...

Locations of Flow Data Changes

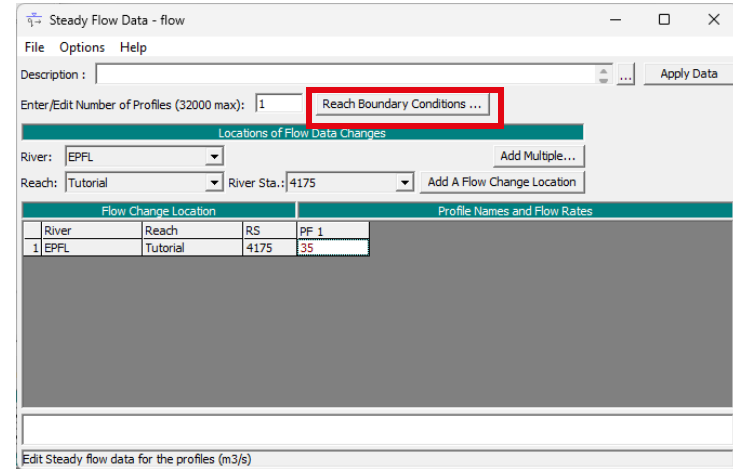
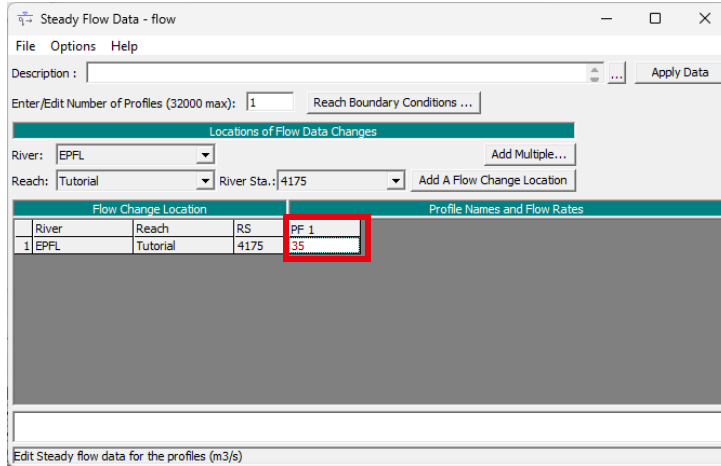
River: EPFL Add Multiple...

Reach: Tutorial River Sta.: 4175 Add A Flow Change Location

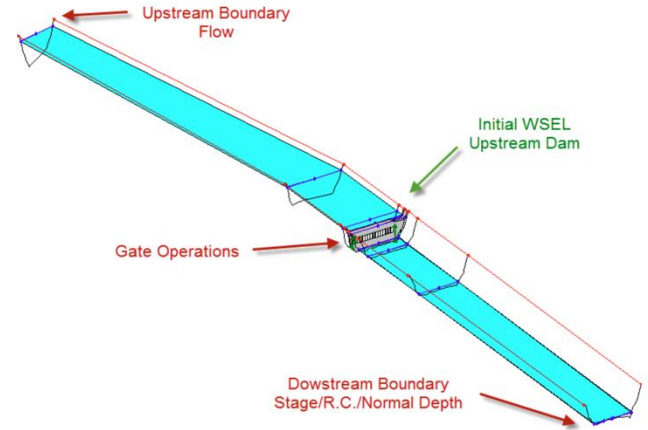
Flow Change Location			Profile Names and Flow Rates	
River	Reach	RS	PF 1	
1 EPFL	Tutorial	4175		

Edit Steady flow data for the profiles (m3/s)

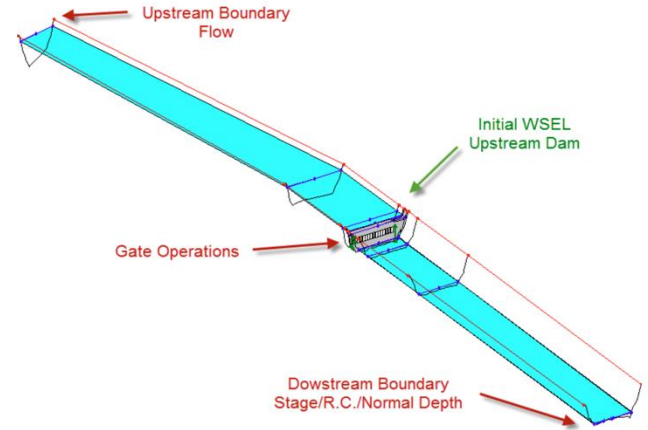
We can try several discharges simultaneously. Now we must enter the Boundary Conditions.



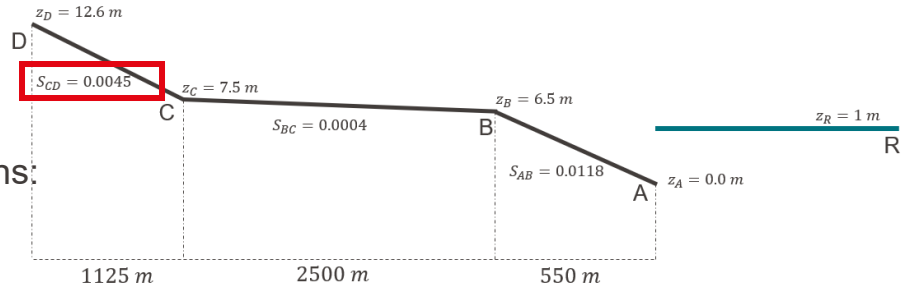
- Define how **flow enters and exits** the modeled system
- Required at **upstream and downstream** ends
- **Upstream Boundary:**
  - Specify **discharge (Q)** for each reach
- **Downstream Boundary:**
  - Specify **water surface or energy condition**, such as:
    - Known water surface elevation
    - Normal depth (energy slope)
    - Rating curve (stage–discharge relationship)
- **Analogy with the Direct Step Method**
  - Both require:
    - **Discharge (Q)** → like the **upstream boundary**
    - **Depth or energy** → like the **downstream boundary**
  - Both compute **gradually varied flow profiles** using known hydraulic states
  - HEC-RAS automates and extends the **Direct Step Method** using detailed geometry and iterative energy balance



- Represent **hydraulic controls or transitions** *within* the modeled reach
- Define how flow behavior changes **between cross sections**
- **Common Internal Conditions:**
  - **Bridges & Culverts:** create local energy losses and flow contractions
  - **Weirs, Spillways, and Gates:** control water levels or flow rates
  - **Junctions / Confluences:** split or combine discharges between reaches
  - **Inline or lateral structures:** alter headwater and tailwater relationships
- **Purpose:**
  - Ensure realistic **energy balance** and **flow continuity** at internal locations
  - Capture effects of **obstructions, control structures, and geometry changes**
- **Key Idea:**
  - While external boundaries set **inlet/outlet conditions**, **internal conditions define what happens in between.**

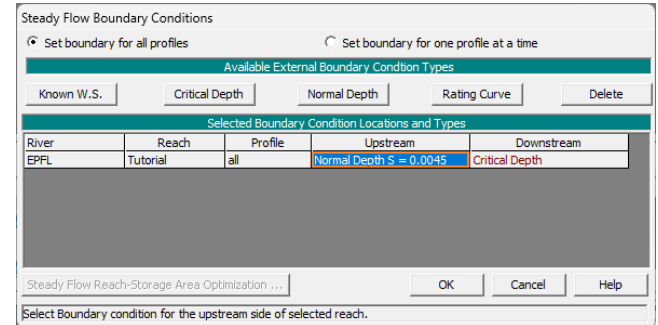
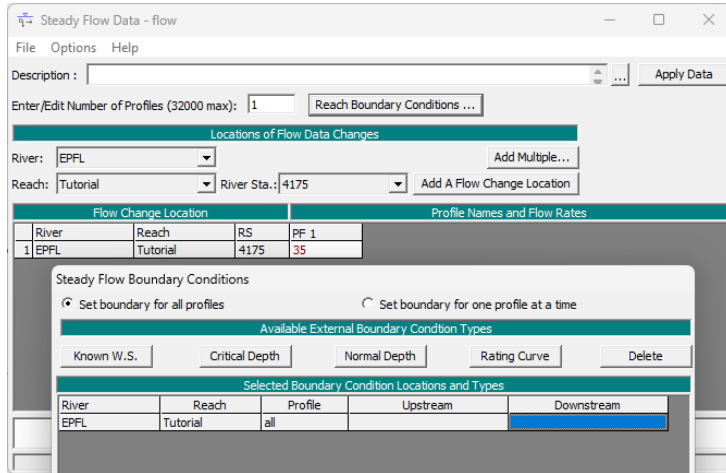


# Boundary Conditions

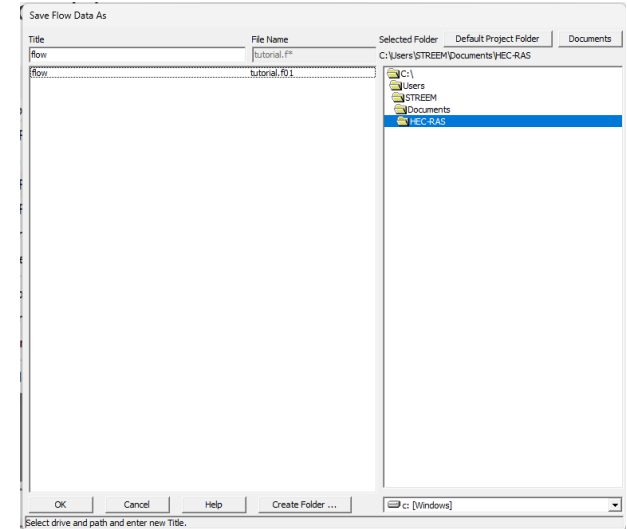
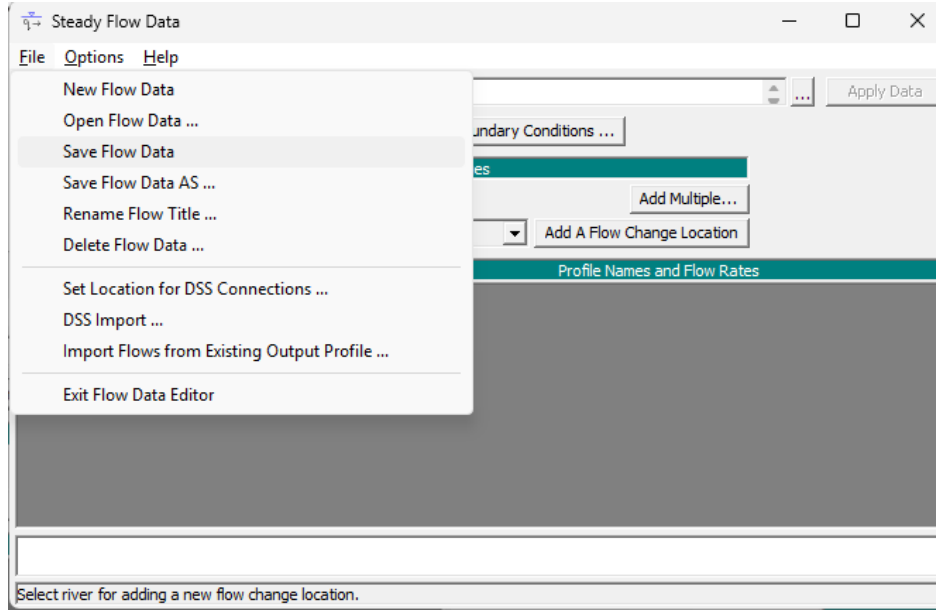


We have different options for Boundary Conditions:

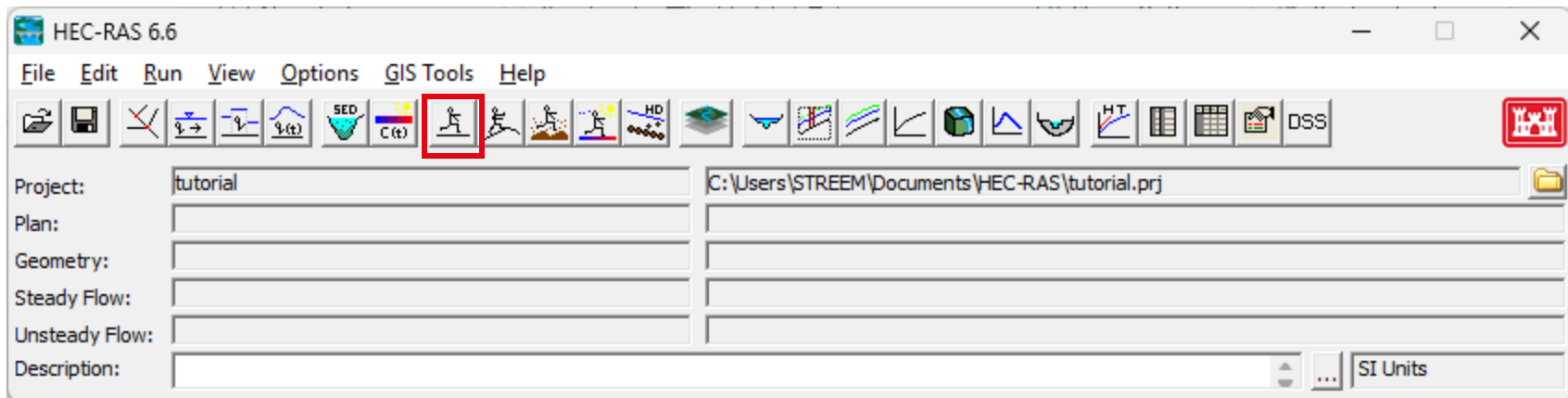
- Known Water Surface level
- Critical Depth
- Normal Depth Requires slope
- Rating Curve ( $Q(h)$ )



We save the flow data

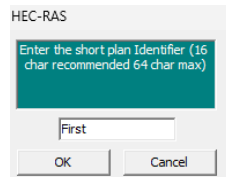
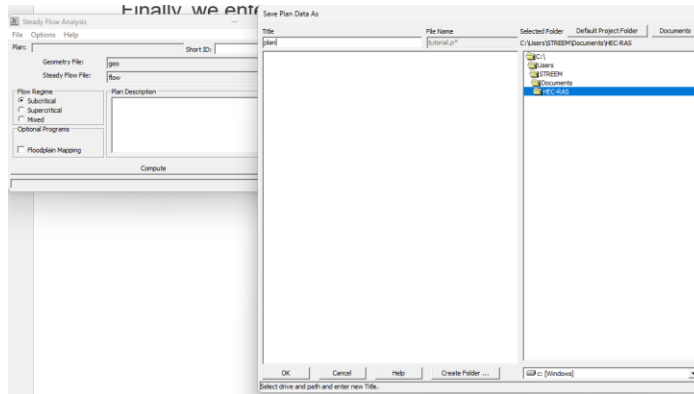


Finally, we enter the “Plan” data



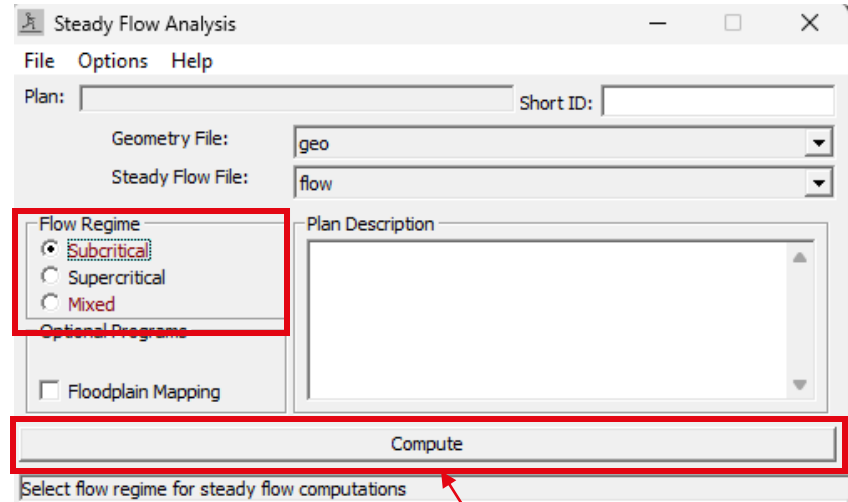
Finally, we enter the “Plan” data

We save it immediately



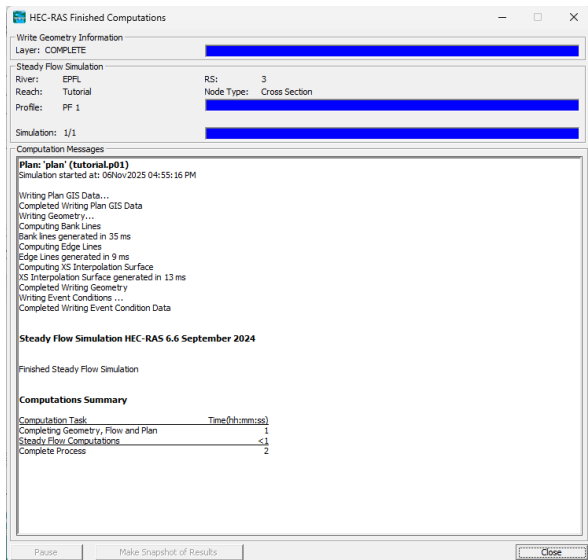
You can name the Case/Plan

Then we choose the Flow Regime

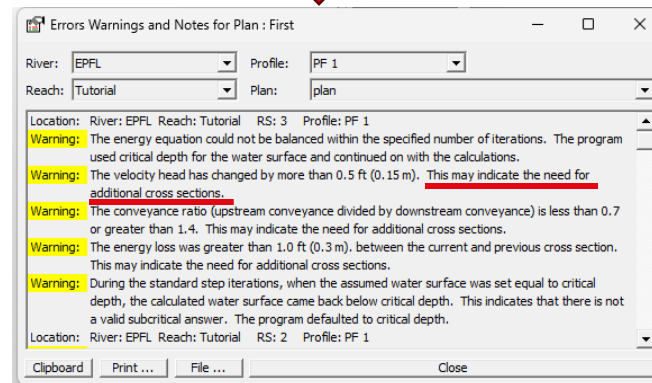
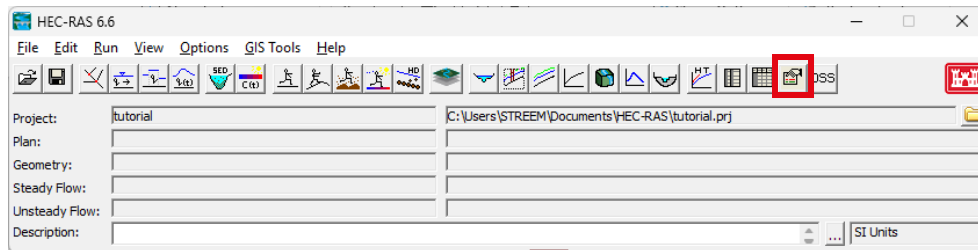


And press “Compute”

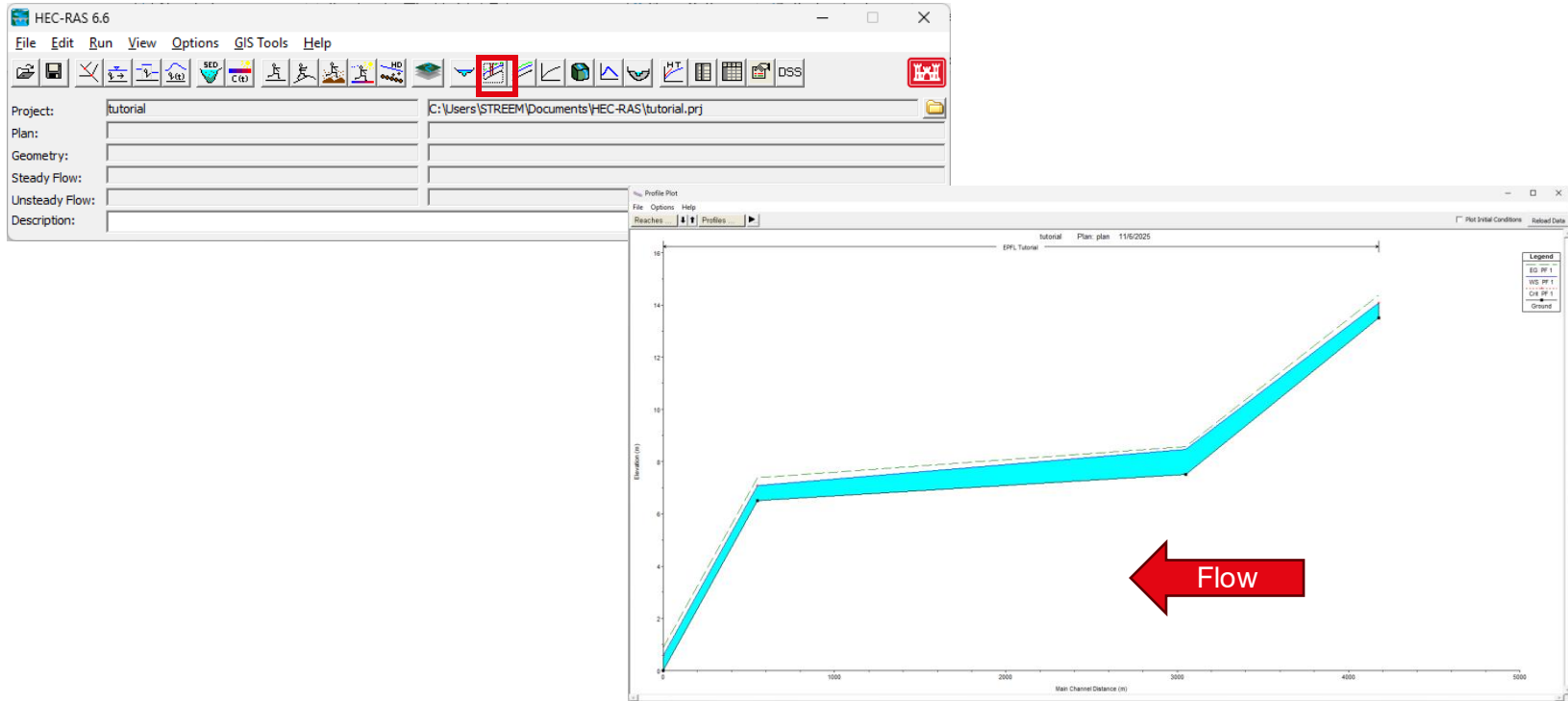
It runs fast because it's 1D



We can check Errors and Warnings

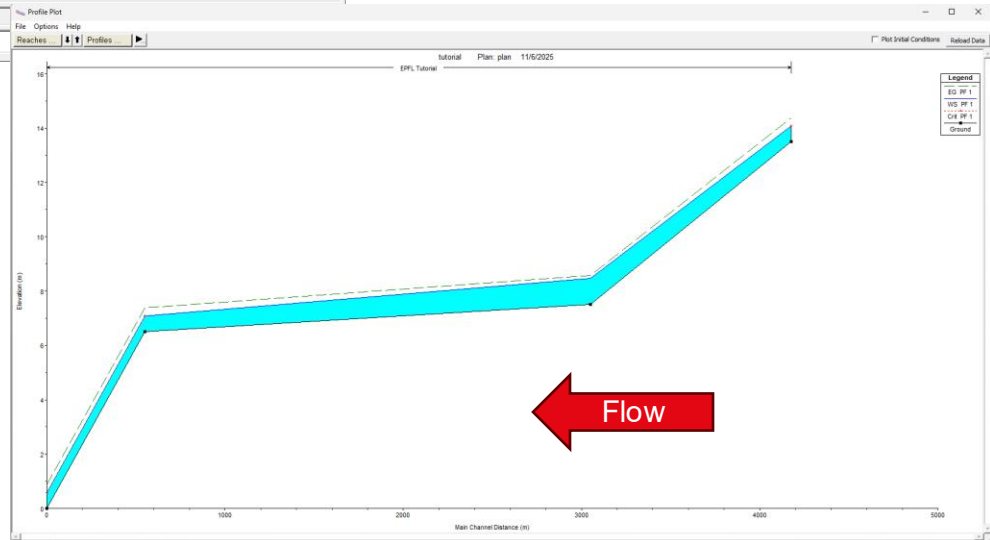
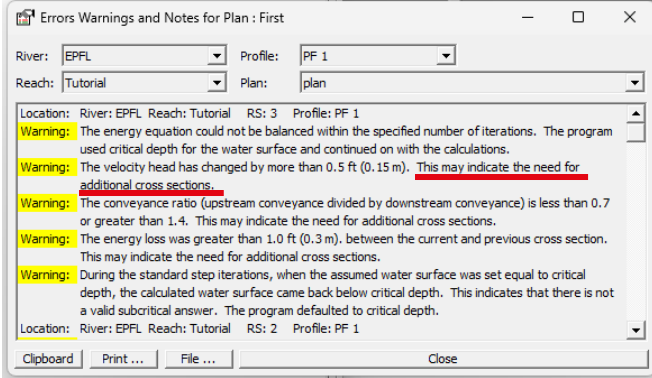
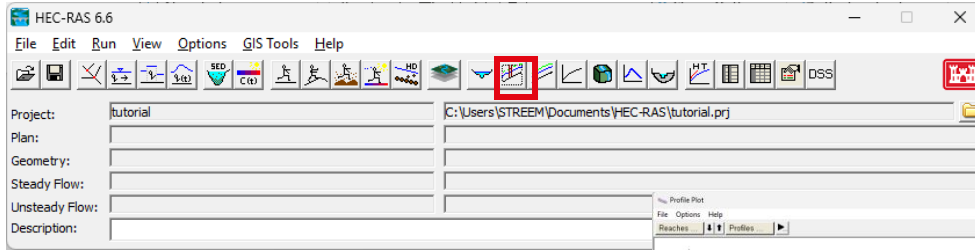


We can see the results:



Doesn't look like expected...

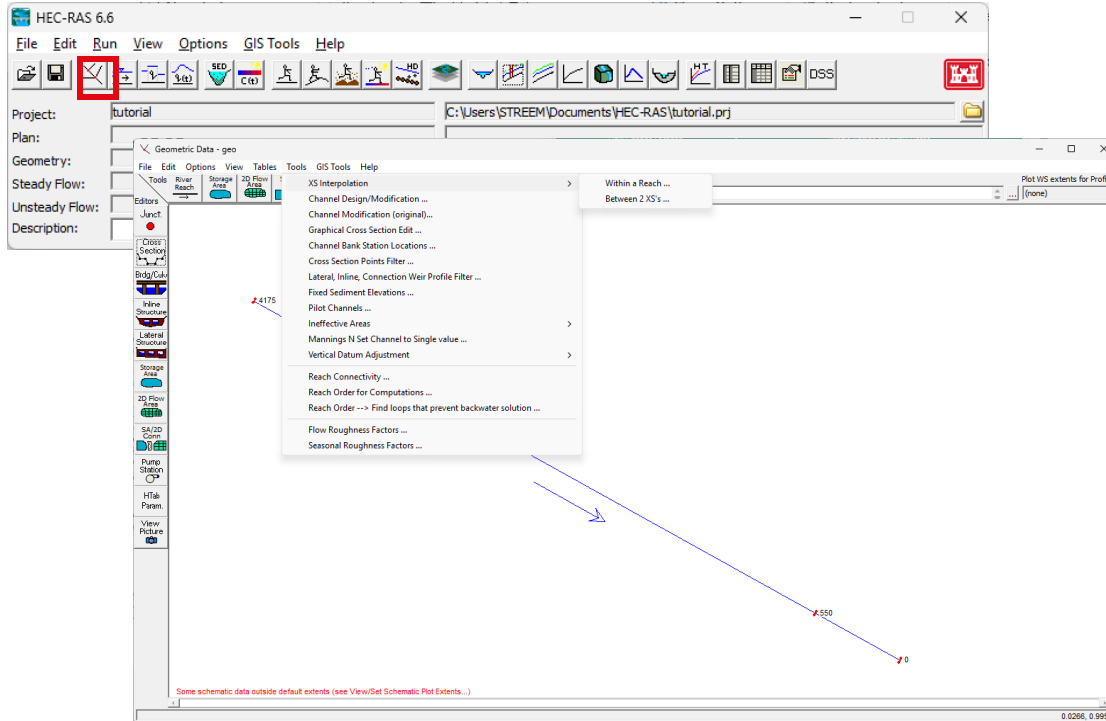
We can see the results:



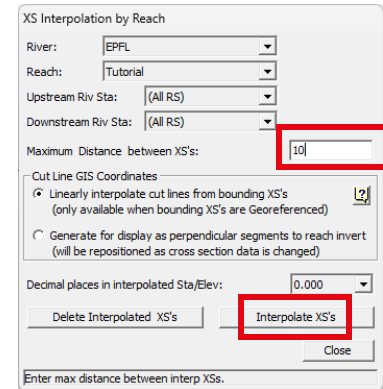
More cross sections :O

Doesn't look like expected...

We go back to Geometry

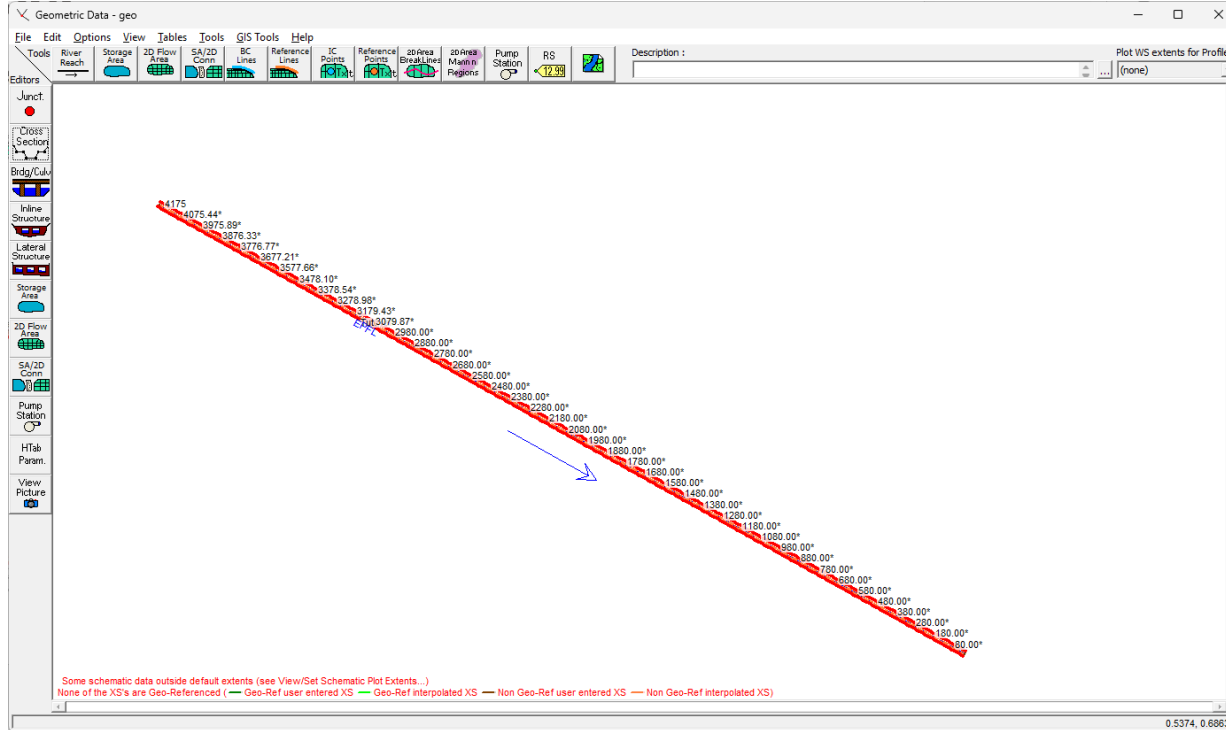


We interpolate Cross Sections (XS's) within a river reach:

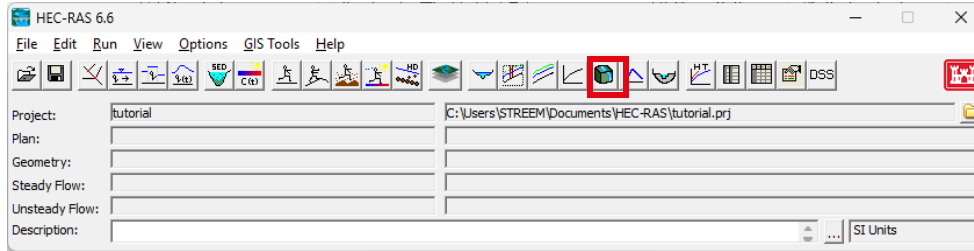


Can be done between 2 XS's only

Many new sections appeared:

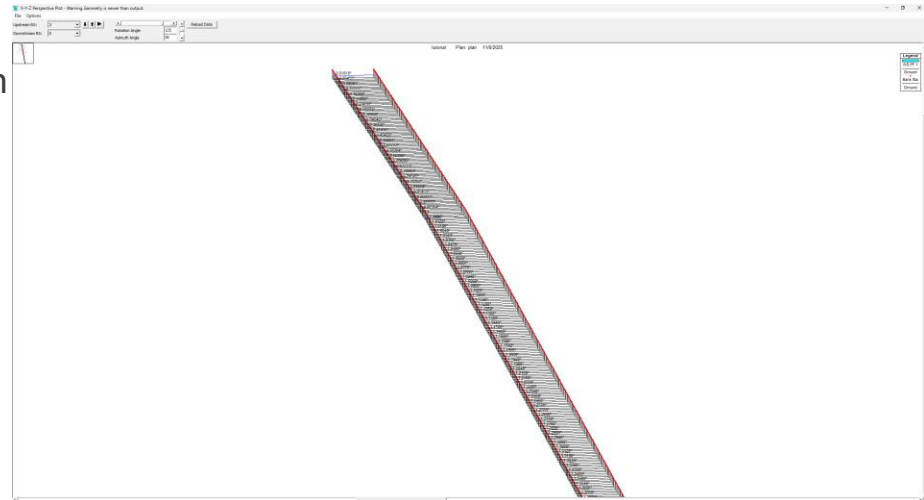


We can look at them in “3D”

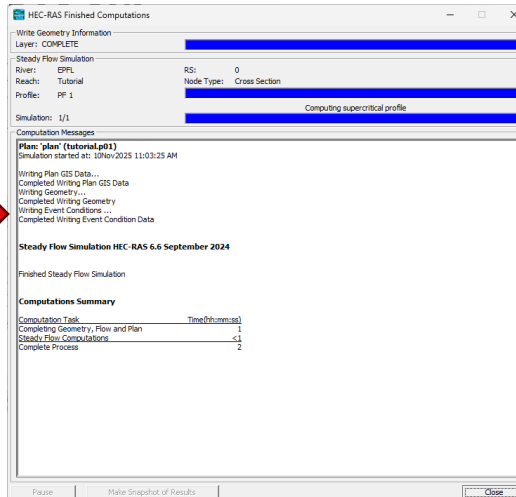
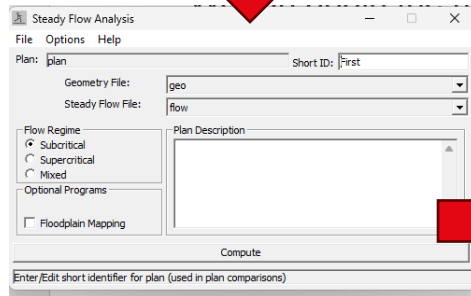
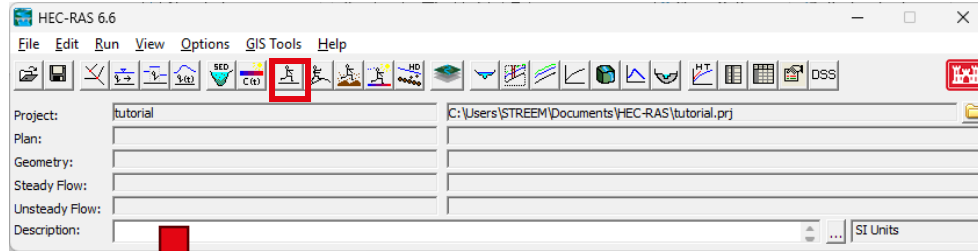


The interpolation is linear between sections  
We must have sections in areas where sudden changes occur. Otherwise, we're unable to capture the physics.

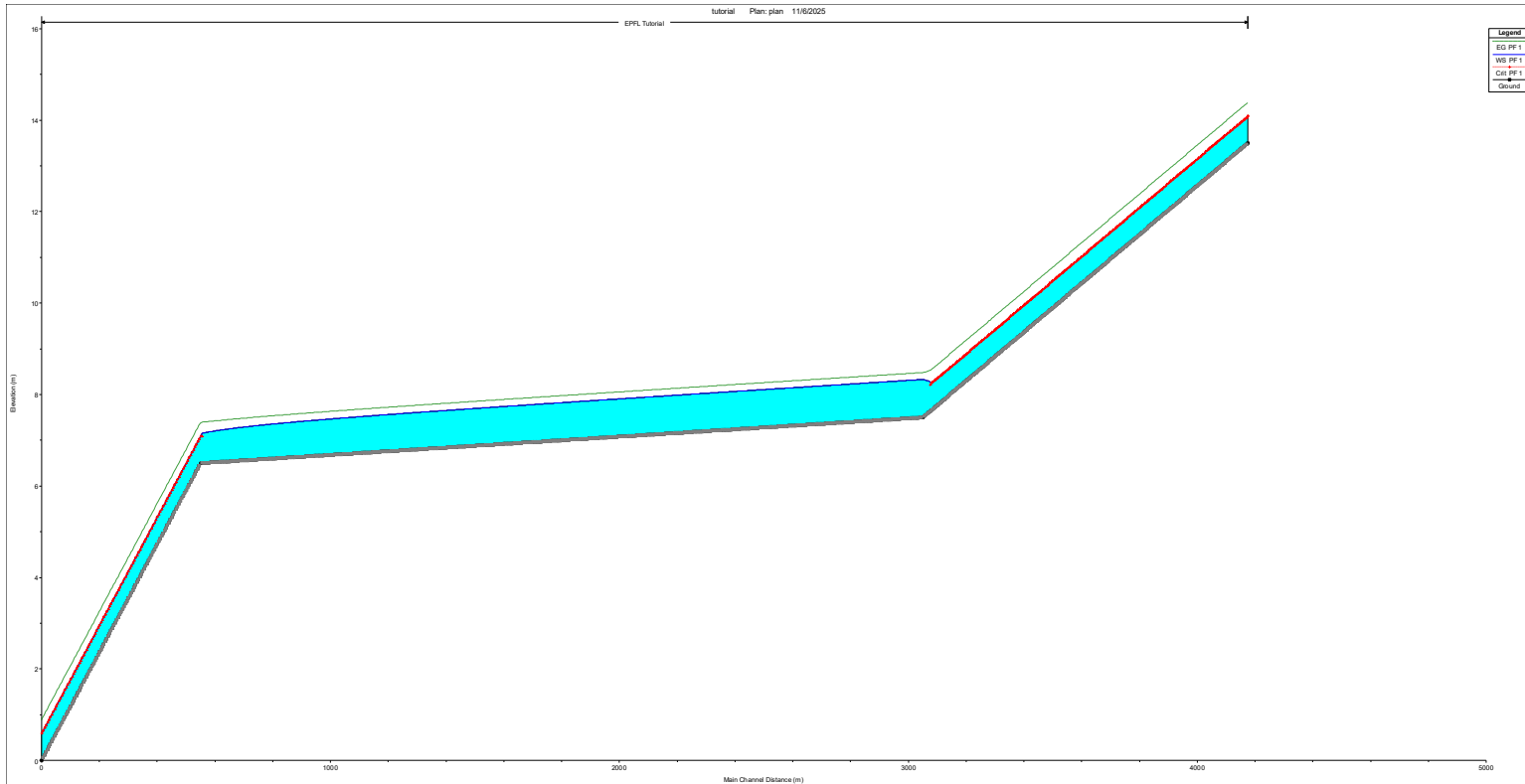
After zooming in and playing with the perspective



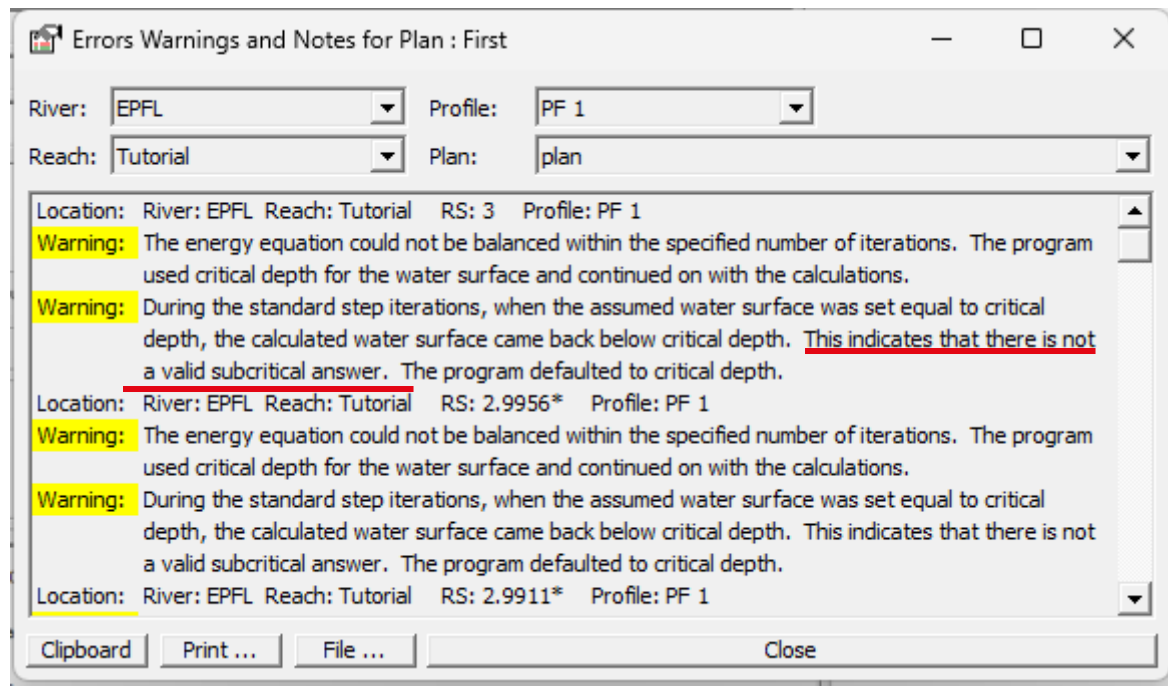
We run again the model

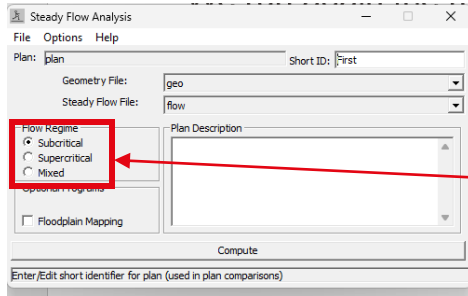


It looks better



But if we check the warnings...

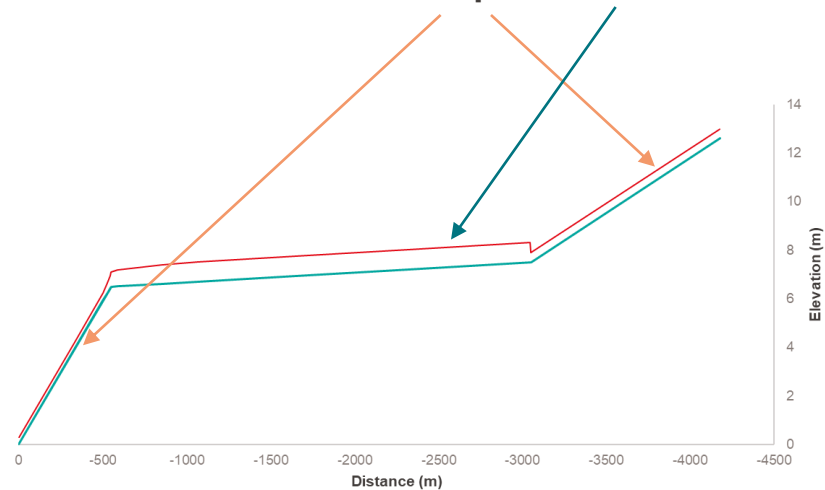




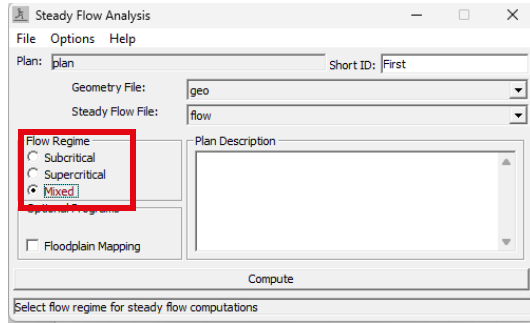
This assumption of subcritical flow everywhere seems to be incorrect :O

Remember how we said the profile should be?

It's a mix between **super** and **sub** critical flows.

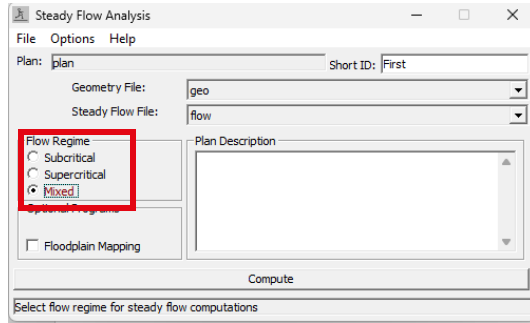


We change it to mixed:



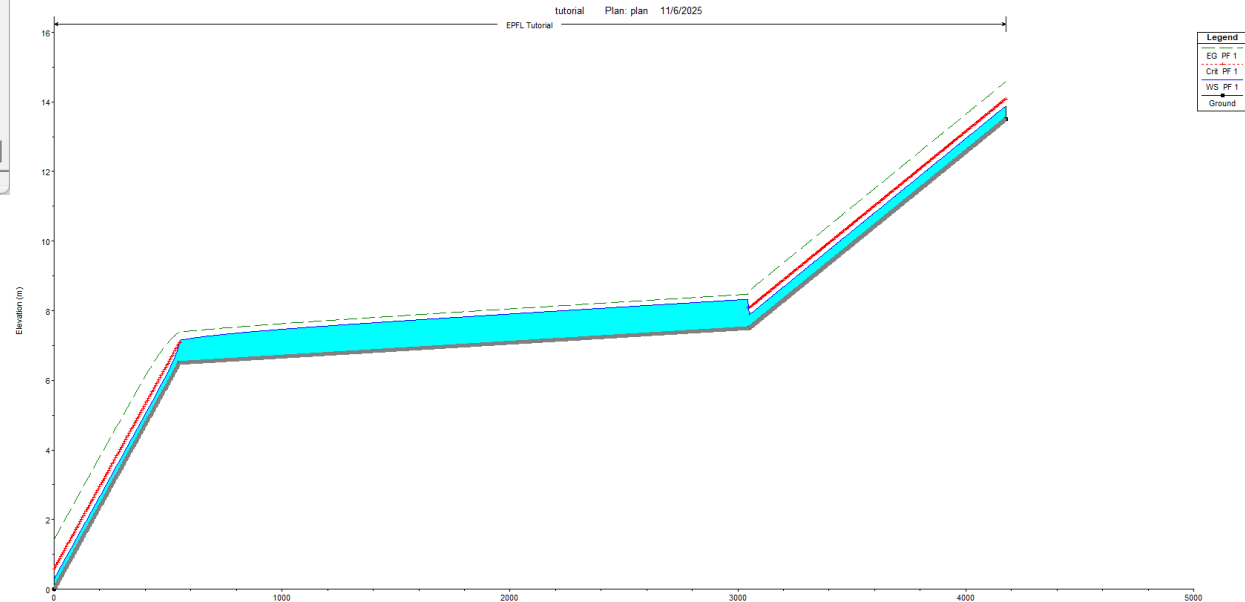
And Compute again.

We change it to mixed:

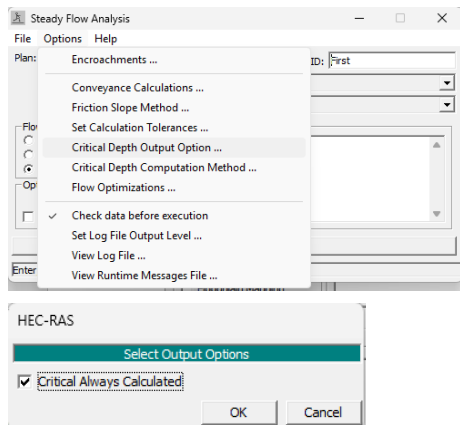


And Compute again.

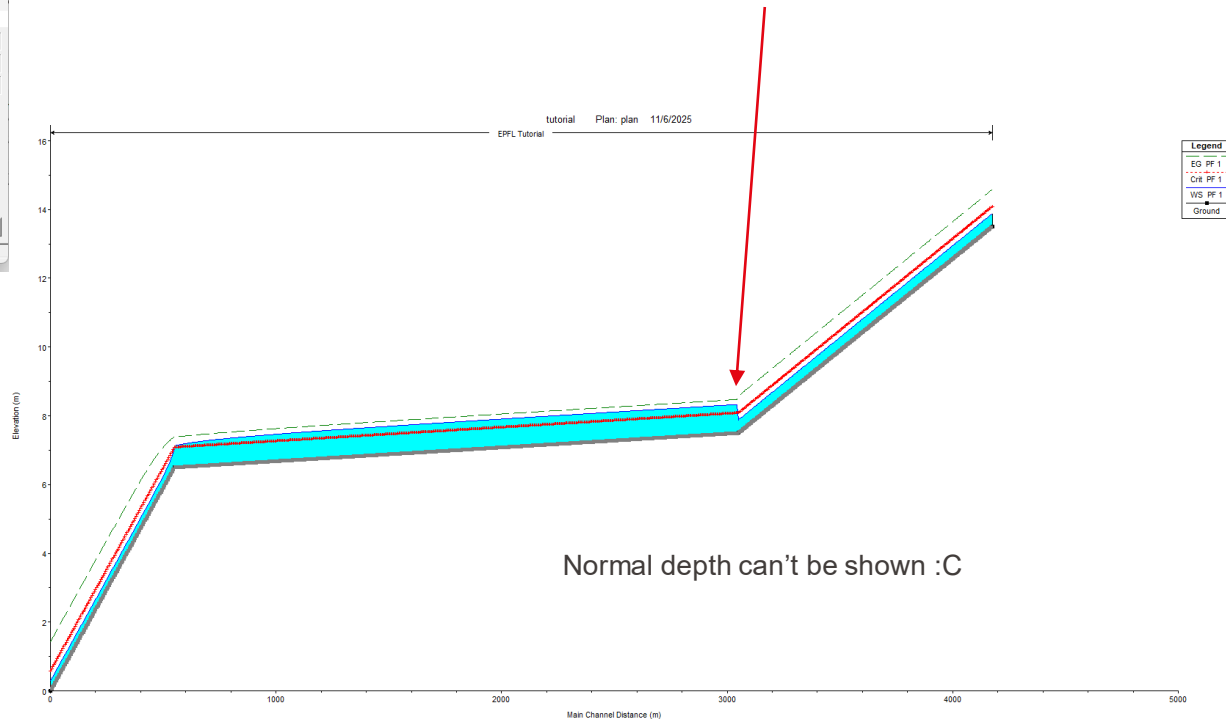
Now it looks as we said:



We can also force the critical depth to show everywhere:



Hydraulic jumps are always plotted between 2 sections only, even if the length is greater than the separation between those 2 XS's



We can get results as table

HEC-RAS 6.6

File Edit Run View Options GIS Tools Help

Project: tutorial C:\Users\STREAM\Documents\HEC-RAS\tutorial.prj

Plan:

Geometry:

Steady Flow:

Unsteady Flow:

Description:

Profile Output Table - Standard Table 1

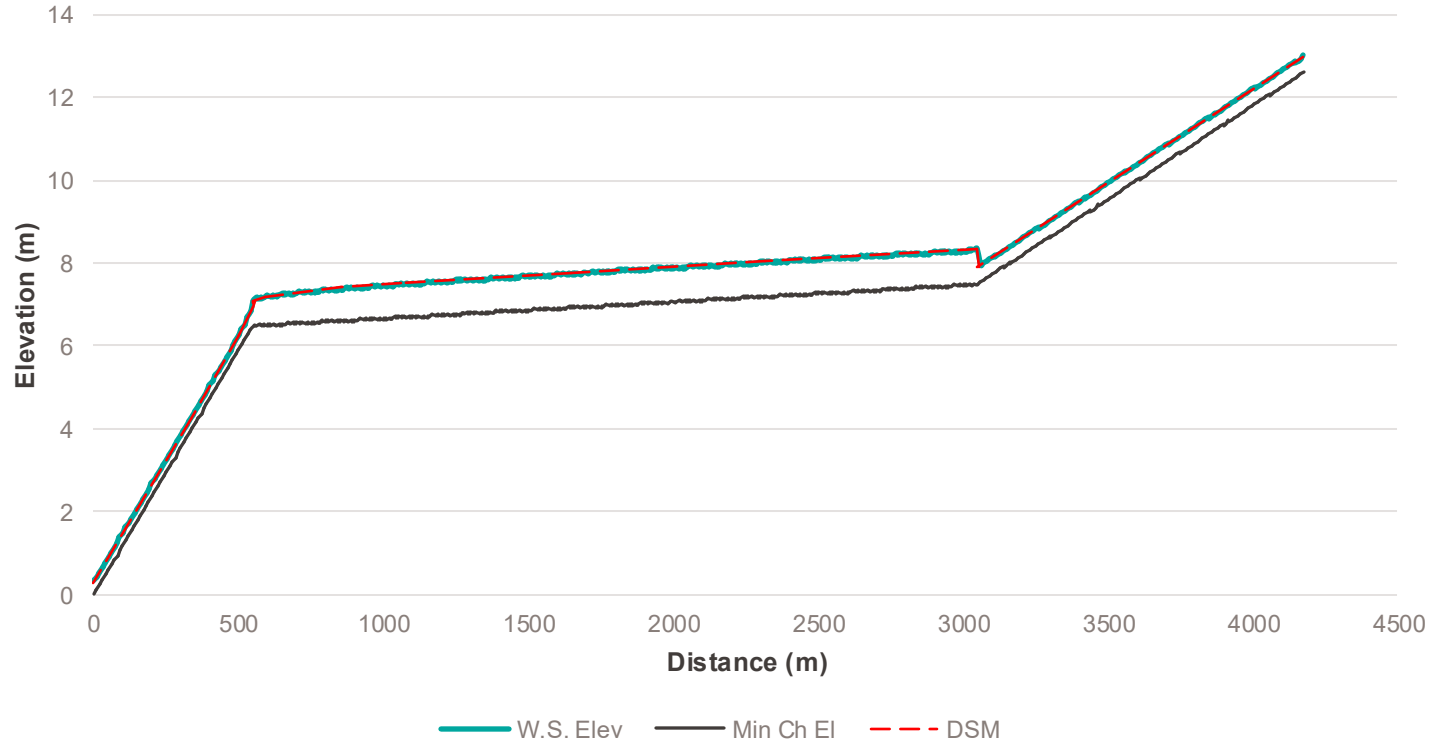
File Options Std. Tables Locations Help

HEC-RAS Plan: First River: EPFL Reach: Tutorial Profile: PF 1

Reach	River Sta	Profile	Q Total (m <sup>3</sup> /s)	Mn Ch El (m)	W.S. Elev (m)	Crit W.S. (m)	E.G. Elev (m)	E.G. Slope (m/m)	Vel Chnl (m/s)	Flow Area (m <sup>2</sup> )	Top Width (m)	Froude # Ch
Tutorial	3	PF 1	35.00	13.50	13.88	14.08	14.58	0.005302	3.72	9.41	25.00	1.94
Tutorial	2.9956*	PF 1	35.00	13.47	13.85	14.06	14.56	0.005315	3.72	9.40	25.00	1.94
Tutorial	2.9911*	PF 1	35.00	13.45	13.82	14.03	14.53	0.005315	3.72	9.40	25.00	1.94
Tutorial	2.9867*	PF 1	35.00	13.42	13.80	14.00	14.50	0.005394	3.72	9.41	25.00	1.94
Tutorial	2.9822*	PF 1	35.00	13.39	13.77	13.98	14.47	0.005277	3.72	9.42	25.00	1.93
Tutorial	2.9778*	PF 1	35.00	13.37	13.74	13.95	14.45	0.005277	3.72	9.42	25.00	1.93
Tutorial	2.9733*	PF 1	35.00	13.34	13.72	13.92	14.42	0.005243	3.71	9.44	25.00	1.93
Tutorial	2.9689*	PF 1	35.00	13.31	13.69	13.90	14.39	0.005219	3.70	9.45	25.00	1.92
Tutorial	2.9644*	PF 1	35.00	13.29	13.67	13.87	14.36	0.005219	3.70	9.45	25.00	1.92
Tutorial	2.9600*	PF 1	35.00	13.26	13.64	13.84	14.33	0.005172	3.69	9.48	25.00	1.92
Tutorial	2.9556*	PF 1	35.00	13.23	13.61	13.82	14.31	0.005208	3.70	9.46	25.00	1.92
Tutorial	2.9511*	PF 1	35.00	13.21	13.59	13.79	14.28	0.005208	3.70	9.46	25.00	1.92
Tutorial	2.9467*	PF 1	35.00	13.18	13.56	13.76	14.25	0.005199	3.69	9.48	25.00	1.91
Tutorial	2.9422*	PF 1	35.00	13.15	13.53	13.74	14.22	0.005119	3.68	9.51	25.00	1.91
Tutorial	2.9378*	PF 1	35.00	13.13	13.51	13.71	14.20	0.005110	3.68	9.51	25.00	1.90
Tutorial	2.9333*	PF 1	35.00	13.10	13.48	13.68	14.17	0.005156	3.69	9.49	25.00	1.91
Tutorial	2.9289*	PF 1	35.00	13.07	13.45	13.66	14.15	0.005195	3.70	9.46	25.00	1.92
Tutorial	2.9244*	PF 1	35.00	13.05	13.43	13.63	14.12	0.005194	3.70	9.47	25.00	1.92
Tutorial	2.9200*	PF 1	35.00	13.02	13.40	13.60	14.09	0.005156	3.69	9.49	25.00	1.91
Tutorial	2.9156*	PF 1	35.00	12.99	13.37	13.58	14.07	0.005194	3.70	9.47	25.00	1.92
Tutorial	2.9111*	PF 1	35.00	12.97	13.35	13.55	14.04	0.005193	3.70	9.47	25.00	1.92
Tutorial	2.9067*	PF 1	35.00	12.94	13.32	13.52	14.02	0.005226	3.70	9.45	25.00	1.92
Tutorial	2.9022*	PF 1	35.00	12.91	13.29	13.50	13.99	0.005177	3.69	9.47	25.00	1.92
Tutorial	2.8978*	PF 1	35.00	12.89	13.27	13.47	13.96	0.005177	3.69	9.47	25.00	1.92
Tutorial	2.8933*	PF 1	35.00	12.86	13.24	13.44	13.93	0.005155	3.68	9.50	25.00	1.91
Tutorial	2.8889*	PF 1	35.00	12.83	13.21	13.42	13.91	0.005177	3.69	9.47	25.00	1.92
Tutorial	2.8844*	PF 1	35.00	12.81	13.19	13.39	13.88	0.005171	3.69	9.48	25.00	1.92
Tutorial	2.8800*	PF 1	35.00	12.78	13.16	13.36	13.86	0.005208	3.70	9.46	25.00	1.92
Tutorial	2.8756*	PF 1	35.00	12.75	13.13	13.34	13.83	0.005168	3.69	9.48	25.00	1.91
Tutorial	2.8711*	PF 1	35.00	12.73	13.11	13.31	13.80	0.005156	3.69	9.49	25.00	1.91
Tutorial	2.8667*	PF 1	35.00	12.70	13.08	13.28	13.77	0.005111	3.68	9.51	25.00	1.90
Tutorial	2.8622*	PF 1	35.00	12.67	13.05	13.26	13.75	0.005157	3.69	9.49	25.00	1.91
Tutorial	2.8578*	PF 1	35.00	12.65	13.03	13.23	13.72	0.005146	3.69	9.49	25.00	1.91
Tutorial	2.8533*	PF 1	35.00	12.62	13.00	13.20	13.70	0.005186	3.70	9.47	25.00	1.92

Total flow in cross section.

And compare with our Direct-Step Method results:



Model the following situation. Which Boundary Conditions do you think are more appropriate for this case? If you double the discharge, how does the Hydraulic Profile change? How would you solve this problem with the Direct-Step Method?

